Phenomenology of a pseudoscalar inflaton: naturally large non-gaussianity

Marco Peloso, University of Minnesota

Neil Barnaby, M.P., PRL 106, 181301 (2011)

Neil Barnaby, Ryo Namba, M.P., JCAP 009, 1104, (2011)

Neil Barnaby, Enrico Pajer, MP, in progress

- Inflation & particle production
- ϕA_{μ} coupling in axion-inflation



detectable non-gaussianity of characteristic (\sim equilateral) shape



+ detectable gravity waves

Inflation is a postulated era of accelerated expansion at $t \ll 1$ s that solves many problems of big-bang cosmology (horizon, flatness, monopole,....) Guth '81, Linde'82, Albrecht and Steinhardt '82

- Simplest source: scalar field ϕ with flat potential $\sim \Lambda$
- $\delta \phi \rightarrow$ inhomogeneities & structures in the universe

Bardeen, Guth, Hawking, Kodama, Mukhanov, Pi, Sasaki, Starobinsky, Steinhardt, Turner, ...





n_s





/smice % fails spine not an entre first a start start at the start water with the boyels at least Made in the second of the sec ince 沢 Local form: $\delta(x) = \delta_{q}(x) + f_{NL}^{\text{local}} \delta_{q}^{2}(x)$ Komatsu. Spergel '01 Nodels with an entropy of the contract of Nodels with a truther the curvature perturbed is a structure of the intervative perturbed in the curvature perturbed in the curv Inflatohihitetonionikitalohitetest and and the state and a state a Models winfrations vant Prenavitational anteraction Vonsaussianty besmall (f_{NL~0.05}) for Orthogonal form, flattened form single field slow roll inflation (potential extremely flat) modulated pfiturbations) have isocusion prediction for adding perceipe inflaton All models at least bations conversion outside horizon, where graduerits are interestanted single field want Rredicted nongaussianity of the local type. $f_{NL}^{equil} < 266$ Inflatonawitek, nomistandard kinetic term: k - kGaussian Medician En nonintercting inflaton 416 Rochatthat least gravitational interaction. Nongaussianity as the small ($\mathcal{P}_{NL\sim0.05}$) for Substantial improvement in near future from CMB (Planck) and LSS single field slow roll inflation (potential extremely flat)

Maldacona '02

• Virtue of inflation: simplest models work !

Single ϕ ; flat V; slow-roll; canonical $(\partial \phi)^2$; standard initial vacuum

• Virtue of inflation: simplest models work !

Single ϕ ; flat V; slow-roll; canonical $(\partial \phi)^2$; standard initial vacuum

Unobservable primordial non-gaussianity $f_{
m NL} \sim 0.02$

 Non-gaussianity ↔ inflaton interactions. Very weakly interacting in simplest cases (gravity, flat V)

• Virtue of inflation: simplest models work !

Single ϕ ; flat V; slow-roll; canonical $(\partial \phi)^2$; standard initial vacuum

Unobservable primordial non-gaussianity $f_{\rm NL} \sim 0.02$

 Non-gaussianity ↔ inflaton interactions. Very weakly interacting in simplest cases (gravity, flat V)

Add a strong coupling !

Eg.
$$V = V(\phi) + g^2 (\phi - \phi_0)^2 \chi^2$$

Chung, Kolb, Riotto, Tkachev '99 Romano, Sasaki '08 Barnaby, Huang, Kofman, Pogosyan '09 Green, Horn, Senatore, Silverstein '09

• Virtue of inflation: simplest models work !

Single ϕ ; flat V; slow-roll; canonical $(\partial \phi)^2$; standard initial vacuum

Unobservable primordial non-gaussianity $f_{\rm NL} \sim 0.02$

 Non-gaussianity ↔ inflaton interactions. Very weakly interacting in simplest cases (gravity, flat V)

Add a strong coupling !	Chung, Kolb, Riotto, Tkachev '99
	Romano, Sasaki '08
Eg. $V = V(\phi) + g^2 (\phi - \phi_0)^2 \chi^2$	Barnaby, Huang, Kofman, Pogosyan '09
	Green, Horn, Senatore, Silverstein '09

- For most of the evolution, $m_\chi \sim g\phi \gg H$, no effect
- At $\phi = \phi_0$, nonadiabatic m_{χ} variation

$$\Rightarrow n_{\chi}(t_0) = \exp\left(-\frac{\pi k^2}{k_*^2}\right) , \quad k_* \equiv g |\dot{\phi}|$$

$$V = V(\phi) + g^2 (\phi - \phi_0)^2 \chi^2$$

Two effects on inflaton (\rightarrow metric) perturbations:

- Inflaton slowed down by the production at ϕ_0
- Rescattering of χ quanta into $\delta\phi$



$$V = V(\phi) + g^2 (\phi - \phi_0)^2 \chi^2$$

Two effects on inflaton (\rightarrow metric) perturbations:

- Inflaton slowed down by the production at ϕ_0
- Rescattering of χ quanta into $\delta\phi$





$$g^2 \lesssim O\left(10^{-2}
ight)$$
 for $10^{-7} \lesssim rac{k_*}{\mathrm{Mpc}^{-1}} \lesssim 10^{-1}$

Barnaby et al '09

Trapped inflation

Green, Horn, Senatore, Silverstein '09 (monodromy)

$$V = \frac{1}{2}m^2\phi^2 + \frac{g^2}{2}\sum (\phi - \phi_i)^2 \chi_i^2$$



Trapped inflation

Green, Horn, Senatore, Silverstein '09

(monodromy)

$$V = \frac{1}{2}m^{2}\phi^{2} + \frac{g^{2}}{2}\sum (\phi - \phi_{i})^{2} \chi_{i}^{2}$$

Continuous production ($\Delta \phi_i$ small):

- Damping controls slow roll
- New source of $\delta\phi$ at all scales



Trapped inflation

Green, Horn, Senatore, Silverstein '09

$$V = \frac{1}{2}m^2\phi^2 + \frac{g^2}{2}\sum (\phi - \phi_i)^2 \chi_i^2$$

Continuous production ($\Delta \phi_i$ small):

- Damping controls slow roll
- New source of $\delta\phi$ at all scales

Estimated bounds:



(monodromy)



• Strong couplings + Loops \rightarrow flatness ?



$$\Delta V = rac{\lambda}{4} \phi^4 \ , \ \lambda \leq 10^{-13}$$

• Strong couplings + Loops \rightarrow flatness ?



• Suggests to limit ϕ couplings. Pessimism for NG ?

• Strong couplings + Loops \rightarrow flatness ?



- Suggests to limit ϕ couplings. Pessimism for NG ?
- Use symmetry. Ex: Shift symmetry for axion inflaton

Single field slow roll inflaton, with controllably flat potential for which coupling to "matter" provides observable non-gaussianity Barnaby, MP '11

QCD axion \rightarrow Inflaton axion

QCD instantons
$$\rightarrow \begin{cases} \Delta \mathcal{L} = \frac{-g^2}{16\pi^2} \theta F \tilde{F} \\ V = \Lambda^4 [1 - \cos\theta] \end{cases}$$

Limit neutron electric dipole moment $\Rightarrow \theta \lesssim 10^{-10}$

QCD axion \rightarrow Inflaton axion

QCD instantons
$$\rightarrow \begin{cases} \Delta \mathcal{L} = \frac{-g^2}{16\pi^2} \theta F \tilde{F} \\ \mathcal{L} = \frac{-g^2}{16\pi^2} \theta F \tilde{F} \end{cases}$$

Limit neutron electric dipole moment $\Rightarrow \theta \lesssim 10^{-10}$

Peccei, Quinn '77: Chiral U(1) symmetry spontaneously broken $\Phi = (f + \rho) e^{i\phi/f}$

Symmetry is anomalous $\Rightarrow \theta \rightarrow \theta + \frac{\phi}{f}$



QCD axion \rightarrow Inflaton axion

QCD instantons
$$\rightarrow \begin{cases} \Delta \mathcal{L} = \frac{-g^2}{16\pi^2} \theta F \tilde{F} \\ \mathcal{L} = \frac{-g^2}{16\pi^2} \theta F \tilde{F} \end{cases}$$

Limit neutron electric dipole moment $\Rightarrow \theta \lesssim 10^{-10}$

Peccei, Quinn '77: Chiral U(1) symmetry spontaneously broken $\Phi = (f + \rho) e^{i\phi/f}$

Symmetry is anomalous $\Rightarrow \theta \rightarrow \theta + \frac{\phi}{f}$



So $\delta \Lambda \propto \Lambda$

• Smallness of Λ is technically natural. No perturbative shift

• ϕ only derivatively coupled

Natural Inflation: Freese, Frieman, Olinto '90





Savage, Freese, Kinney '06

Natural Inflation: Freese, Frieman, Olinto '90



Savage, Freese, Kinney '06

Problems with $f > M_p$

- $U(1)_{PQ}$ broken above QG scale
- Hard in weakly coupled string theory

Kallosh, Linde, Linde, Susskind '95

Banks, Dine, Fox, Gorbatov '03

Two axions & gauge groups Kim, Nilles, MP '04

$$V = \Lambda_1^4 \left[1 - \cos\left(\frac{\theta}{f_1} + \frac{\rho}{g_1}\right) \right] + \Lambda_2^4 \left[1 - \cos\left(\frac{\theta}{f_2} + \frac{\rho}{g_2}\right) \right]$$

 $f_{\text{eff}} >> f,g$ if $f_1/g_1 \simeq f_2/g_2$



Two axions & gauge groups Kim, Nilles, MP '04

$$V = \Lambda_1^4 \left[1 - \cos\left(\frac{\theta}{f_1} + \frac{\rho}{g_1}\right) \right] + \Lambda_2^4 \left[1 - \cos\left(\frac{\theta}{f_2} + \frac{\rho}{g_2}\right) \right]$$

 $f_{\rm eff} >> f,g$ if $f_1/g_1 \simeq f_2/g_2$

N-flation Dimopoulos et al '05

Collectively drive inflation, $f_{\rm eff} = \sqrt{N} f$



$$V = \Lambda_1^4 \left[1 - \cos\left(\frac{\theta}{f_1} + \frac{\rho}{g_1}\right) \right] + \Lambda_2^4 \left[1 - \cos\left(\frac{\theta}{f_2} + \frac{\rho}{g_2}\right) \right]$$

 $f_{\rm eff} >> f,g$ if $f_1/g_1 \simeq f_2/g_2$



N-flation Dimopoulos et al '05

Collectively drive inflation, $f_{\rm eff} = \sqrt{N} f$

Axion monodromy

 $\Delta V \propto \phi$ from brane wrapping

McAllister, Silverstein, Westphal '08 Flauger et al '09 Two axions & gauge groups Kim, Nilles, MP '04

$$V = \Lambda_1^4 \left[1 - \cos\left(\frac{\theta}{f_1} + \frac{\rho}{g_1}\right) \right] + \Lambda_2^4 \left[1 - \cos\left(\frac{\theta}{f_2} + \frac{\rho}{g_2}\right) \right]$$

 $f_{\rm eff} >> f,g$ if $f_1/g_1 \simeq f_2/g_2$



N-flation Dimopoulos et al '05

Collectively drive inflation, $f_{\rm eff} = \sqrt{N} f$

Axion monodromy

McAllister, Silverstein, Westphal '08 Flauger et al '09

Dante's inferno Berg, Pajer, Sjors '09

 $\Delta V \propto \phi$ from brane wrapping

Axion-4form mixing Kaloper, Sorbo '08

Controllable realizations of large field inflation $(V \propto \phi, \phi^2)$, with $f \ll M_p$

$$\mathcal{L} \supset -\frac{lpha}{f} \phi F \tilde{F}$$

- Dictated by shift-symmetry and parity
- Generally present, not "extra ingredient"



$$\mathcal{L} \supset -\frac{lpha}{f} \phi F \tilde{F}$$

- Dictated by shift-symmetry and parity
- Generally present, not "extra ingredient"



• $\varphi^{(0)} \rightarrow A + A$, non-perturbative depletion $\propto \dot{\varphi}^{(0)}$ \implies Exponential growth of A



$$\mathcal{L} \supset -\frac{lpha}{f} \phi F \tilde{F}$$

- Dictated by shift-symmetry and parity
- Generally present, not "extra ingredient"





$$\mathcal{L} \supset -\frac{lpha}{f} \phi F \tilde{F}$$

- Dictated by shift-symmetry and parity
- Generally present, not "extra ingredient"





$$\mathcal{L} \supset -\frac{1}{4}F^2 - \frac{\alpha}{f}\phi^{(0)} F \tilde{F}$$

Classical motion $\phi^{(0)}(t)$ affects

dispersion relations of \pm helicities

$$\mathcal{L} \supset -\frac{1}{4}F^2 - \frac{\alpha}{f}\phi^{(0)} F \tilde{F}$$

Classical motion $\phi^{(0)}(t)$ affects

dispersion relations of \pm helicities

The eigefrequency of one helicity (say A_+ , for $\dot{\phi}^{(0)} > 0$) becomes tachyonic for a H > k, namely after horizon crossing

$$\mathcal{L} \supset -\frac{1}{4}F^2 - \frac{\alpha}{f}\phi^{(0)} F \tilde{F}$$

Classical motion $\phi^{(0)}(t)$ affects

dispersion relations of \pm helicities

The eigefrequency of one helicity (say A_+ , for $\dot{\phi}^{(0)} > 0$) becomes tachyonic for a H > k, namely after horizon crossing







\implies Significant contribution to $\delta \varphi$!

$$\phi^{(0)} + \delta \phi$$
, $\delta A_{A\mu}$, $g_{\mu\nu} + \delta g_{\mu\nu}$
• Above triffnear vertex is $\propto \frac{\alpha}{f}$
for $\frac{\alpha}{f} \gg \frac{1}{M_p} \int_{A}^{A}$

Ignore gravitational interactions



- $\phi^{(0)} + \delta \phi \ , \ \delta A_{\mu} \ , \ g_{\mu\nu} + \delta g_{\mu\nu}$ $\text{Above triffnear vertex is } \propto \frac{\alpha}{f} \qquad \text{Ignore gravitational interactions}$ $\text{for } \frac{\alpha}{f} \gg \frac{1}{M_p} \int_{A}^{A_{\mu}}$
- In $\delta g_{ij,\text{scalar}=0}$ gauge, at leading order in slow roll

$$\left[\partial_{\tau}^{2} + 2\mathcal{H}\partial_{\tau} - \nabla^{2} + \left(a^{2}m^{2} - \frac{3\phi'^{2}}{M_{p}^{2}}\right)\right]\delta\phi = \frac{\alpha}{f}a^{2}\vec{E}\cdot\vec{B}$$

• Curvature pert. on uniform density hypersurfaces $\zeta = -\frac{H}{\dot{\phi}^{(0)}} \delta \phi$

$$\left[\partial_{\tau}^{2} + 2\mathcal{H}\partial_{\tau} - \nabla^{2} + \left(a^{2}m^{2} - \frac{3\phi'^{2}}{M_{p}^{2}}\right)\right]\delta\phi = \frac{\alpha}{f}a^{2}\vec{E}\cdot\vec{B}$$

 $\delta\phi = \delta\phi_{\rm Vacuum} + \delta\phi_{\rm inv.decay}$

$$\left[\partial_{\tau}^{2} + 2\mathcal{H}\partial_{\tau} - \nabla^{2} + \left(a^{2}m^{2} - \frac{3\phi'^{2}}{M_{p}^{2}}\right)\right]\delta\phi = \frac{\alpha}{f}a^{2}\vec{E}\cdot\vec{B}$$

$$\delta \phi = \delta \phi_{\text{vacuum}} + \frac{\delta \phi_{\text{inv.decay}}}{1}$$

Homogeneous solution,

standard cosmological pert.



• Operatorial nature of $\delta\phi_{{
m inv.decay}}$ from A (through \widehat{J}_k)

$$\Rightarrow \langle \delta \phi_{\text{vacuum }} \delta \phi_{\text{inv.decay}} \rangle = 0$$

Namely, $\langle \delta \phi^2 \rangle = \langle \delta \phi^2_{\rm vac} \rangle + \langle \delta \phi^2_{\rm inv.dec} \rangle$, $\langle \delta \phi^3 \rangle = \langle \delta \phi^3_{\rm vac} \rangle + \langle \delta \phi^3_{\rm inv.dec} \rangle$

$$P_{\zeta}(k) = \mathcal{P}_{v}\left(\frac{k}{k_{0}}\right)^{n_{s}-1} \left[1 + 7.5 \cdot 10^{-5} \mathcal{P}_{v} \frac{\mathrm{e}^{4\pi\xi}}{\xi^{6}}\right]$$

 $\mathcal{P}_v^{1/2} \equiv \frac{H^2}{2\pi |\dot{\phi}|}$ $\xi \equiv \frac{\alpha}{f} \frac{|\dot{\phi}|}{2H}$



$$\langle \zeta_{\mathbf{k}_1} \zeta_{\mathbf{k}_2} \zeta_{\mathbf{k}_3} \rangle \propto k_1^{-6} x_2^2 x_3^2 S(x_2, x_3) , \ x_i \equiv \frac{k_i}{k_1}$$

Axion Inflation

1 0.8 0.98 0.6 0.92 ž х 0.4 0.84 0.2 0.6 0.25 0______0.5 0.6 0.7 0.8 0.9 1 **x**₂

Equilateral template



$$\langle \zeta_{\mathbf{k}_1} \zeta_{\mathbf{k}_2} \zeta_{\mathbf{k}_3} \rangle \propto k_1^{-6} x_2^2 x_3^2 S(x_2, x_3) , \ x_i \equiv \frac{k_i}{k_1}$$



Equilateral template



Backreaction

• $\xi \simeq 20$ to obtain slow roll from energy dissipation into A_{μ}

Anber, Sorbo '09

- $\xi \lesssim 2.5$ from NG. No backreaction when CMB perturbations produced
- $\xi \propto \dot{\phi}/H$, can increase during inflation

Ex: $V = \mu^3 \phi$ (case shown here)

extra N = 10 e-folds if $\xi_{in} \simeq 2, 5$.



However, 60 e-folds from $\phi_{\rm in}^{(0)} \simeq 10 M_p$ rather than $\simeq 11 M_p$. Increased n_{s-1}, r

 $V \propto \phi^p \;,\; p = 1,2$ ($\xi \propto 1/f$)



 $V \propto \phi^p \;,\; p = 1,2$ ($\xi \propto 1/f$)



0.02

0.025

0.03

0.04

 $f/\alpha M_{n}$

0.045

0.035

0.05 0.055

0.06

realizations of axion inflation

- Gauge quanta also produce GW. $P_{h,AA} \ll P_{h,vac}$ when NG limit respected Barnaby, Peloso '11
- If ξ grows sufficiently during inflation, potential LIGO / LISA signal Cook, Sorbo '11



Conclusions

- Mechanism for large nongaussianity in models of single slowly rolling inflaton, with controllably flat poential
- Distinctive, and observable, phenomenology



• Already now, $rac{f}{lpha}\gtrsim 10^{16}\,{
m GeV}$

(\sim 5 orders of magnitude stronger than limit on QCD axion-photon coupling)