

The SAURON project – IV. The mass-to-light ratio, the virial mass estimator and Fundamental Plane of elliptical and lenticular galaxies

Michele Cappellari et al. (2006)

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# Topics

- Goal (the purpose of this study)
- Introduction (basic knowledge in this study)
- Sample & data (sample and data used in this study)
- Method (method to estimate  $M/L$ )
- Results
- Summary

# ▪ Goal

~What is the purpose of this study? ~

They investigate the well-known correlations between the dynamical mass-to-light ratio and other global observables (ex . Effective radius , Velocity dispersion , Surface brightness) of E and S0 galaxies.



They want to investigate ...

- whether  $M/L$  is linked to the galaxy dynamics
- a second parameter in the  $M/L$  variations

# ▪ Introduction

- (1) The SAURON project
- (2) Observational example
- (3) Fundamental Plane (FP)

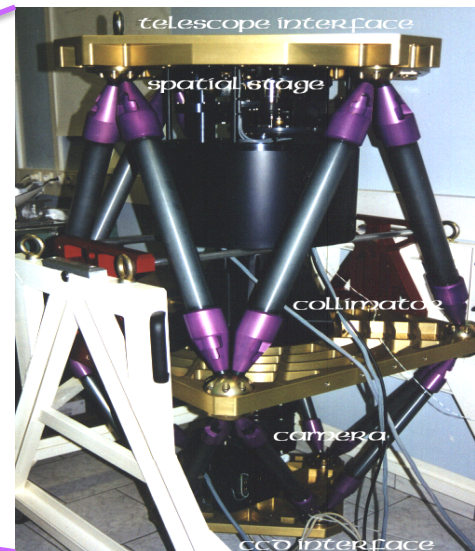
# Introduction(1)

~What is the SAURON project?~

SAURON=Spectrographic Areal Unit for Research on Optical Nebulae



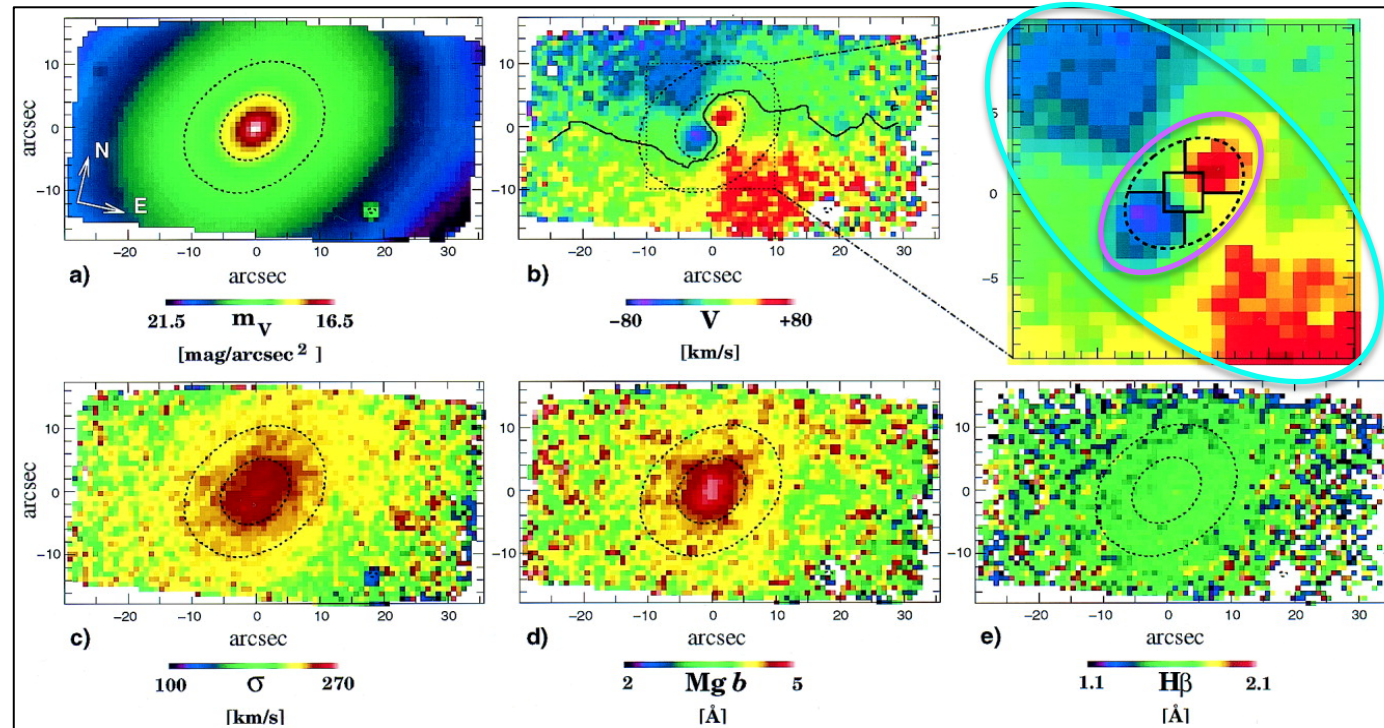
- SAURON is a dedicated instrument , mounted on the William Herschel Telescope (WHT) on La Palma.
- SAURON is designed for studies of the stellar kinematics , gas kinematics , and line-strength distribution of nearby spheroids.



<http://www.strw.leidenuniv.nl/sauron/>

# Introduction (2)

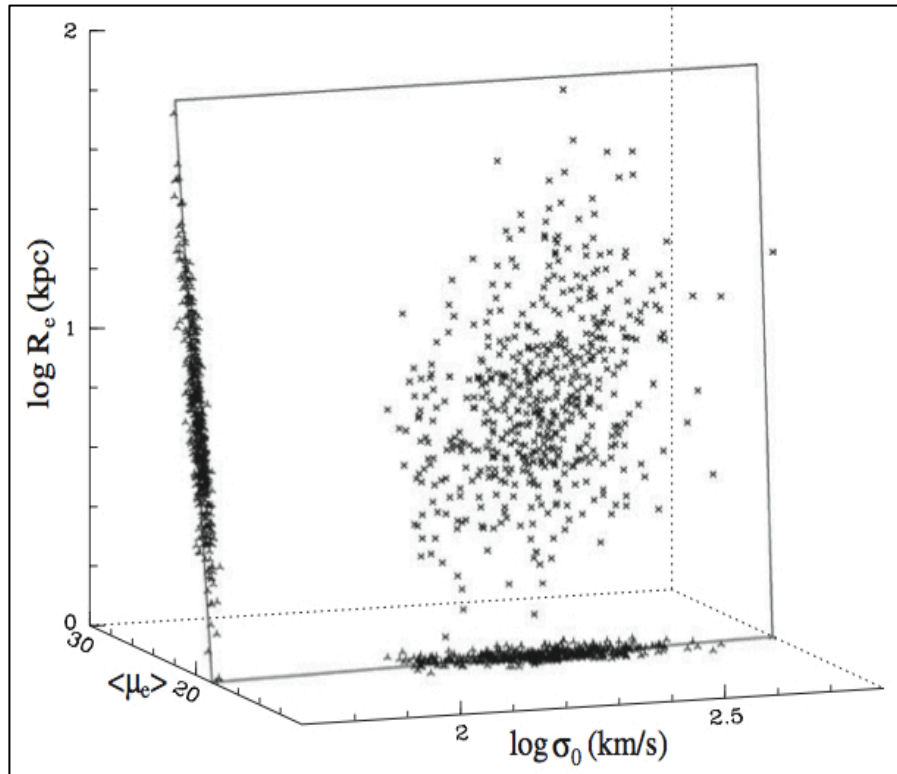
~Observational example~



- These panels are observational examples of SAURON project.
- The top right panel clearly reveal the inner (outer) kinematic component, rotating around the photometric minor axis (major axis).
- The bottom panels reveal the distribution of the velocity dispersion and the line-strengths.
- If you had known about these detailed results, you should read Davies et al. (2001).

# Introduction (3)

~ Fundamental Plane (FP) ~



- This figure is the fundamental plane of elliptical galaxies.
- $\log(R_e) = \alpha \log(\sigma_0) + \beta \log(\langle \mu_e \rangle) + C$   
 $\downarrow$   
 $R_e \propto \sigma_0^\alpha \langle \mu_e \rangle^\beta$
- There is **not correlation** between the velocity dispersion and the effective radius.
- The correlation of the physical quantity of two pieces is **the projection** to the 2-dimensional plane of 3-dimensional distribution.

\* If the profile of surface brightness is a de Vaucouleurs profile ,

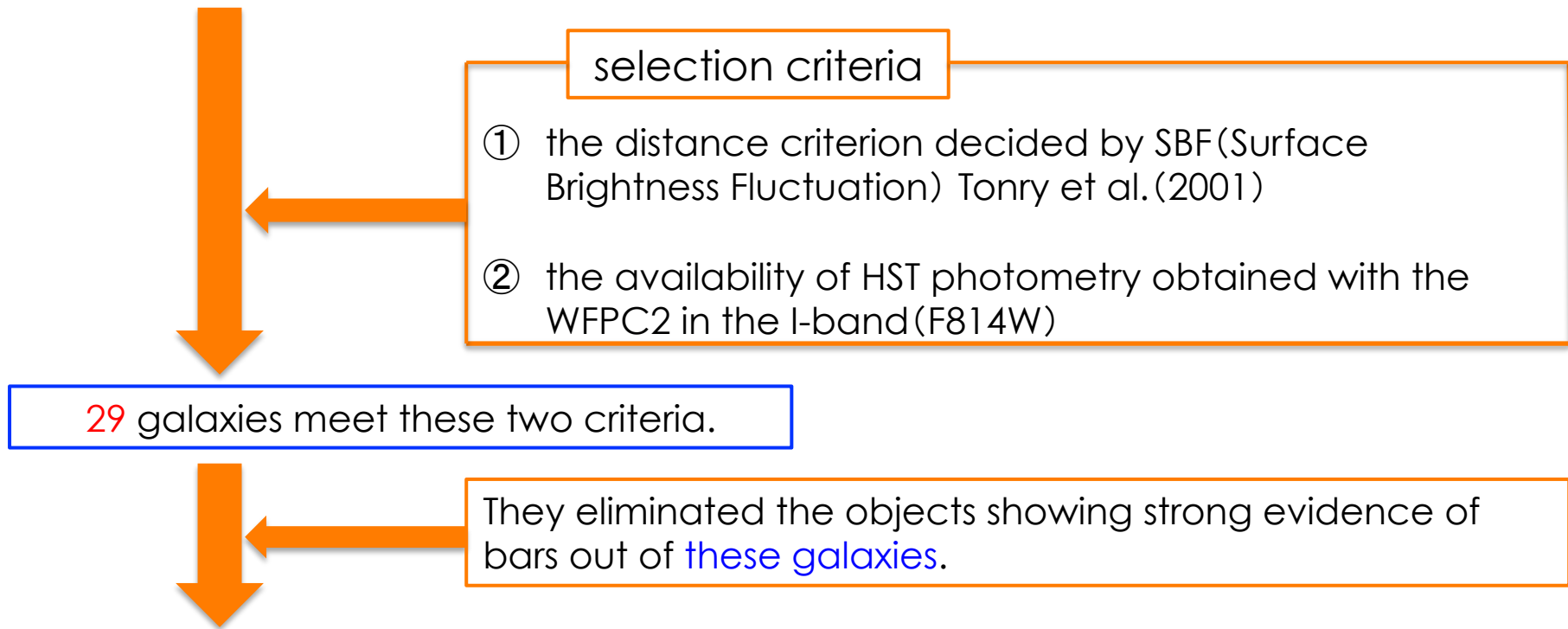
$$L_{\text{tot}} = \int_0^\infty \mu(r) 2\pi r dr = 7.215 \pi r_e^2 \mu_e$$

$$\langle \mu_e \rangle = 3.61 \mu_e$$

# Sample & data

## ~Selection~

The set of galaxies they use for this study was extracted from the SAURON sample of 48 E and S0 galaxies which contain 24 galaxies in each of the E and S0 subclasses. (redshift range:  $z \leq 1$ ,  $M_B \leq -18$  [mag], spans over a factor of 100 in mass)



The 24 galaxies remain. For exploring the low-mass range, they added M32 which is not the SAURON sample to the remaining sample of 24 galaxies.

Finally the 25 galaxies are adopted as a sample of this study.



# ▪ Method

(1) Method to estimate  $(M/L)_{\text{Jeans}}$

(2) Influence of a dark matter halo

(3) Method to estimate  $(M/L)_{\text{Schw}}$

(4) Method to estimate  $(M/L)_{\text{pop}}$

# Method(1)

~Method to estimate  $(M/L)_{\text{Jeans}}$  ~

- For an axisymmetric Jeans model with constant  $M/L$ , and a stellar distribution function (DF) depends only on **two integrals** of motion  $f=f(E, L_z)$ . (Emsellem et al. (1994))
- The **second velocity moment**  $\mu_2$  is a model prediction for  $M/L=1$  and a function of only two free parameters,  $i$  and  $M/L$ .
- They constructed axisymmetric Jeans models for the 25 galaxies in their sample and computed the model predictions for  $\mu_2$  at different inclinations.

$$\left| \begin{array}{l} d_n = \frac{\mu'_{2,n}}{\Delta\mu'_{2,n}} \quad \text{and} \quad m_n = \frac{\mu_{2,n}}{\Delta\mu'_{2,n}} \\ \text{where } \mu'_{2,n} \equiv \sqrt{V_n^2 + \sigma_n^2} \end{array} \right| \quad \left( \frac{M}{L} \right)_{\text{Jeans}} = \left( \frac{d \cdot d}{d \cdot m} \right)^2$$

derived from the SAURON stellar kinematics

# Method (2)

~Influence of a dark matter halo~

- They assume the galaxy to be spherically symmetric and the stellar density to be described by a Hernquist profile

$$\rho_{\star}(r) = \frac{1}{2\pi} \frac{1}{r(r+1)^3}$$

- The Dark Matter contribution is represented by a logarithmic potential

$$\Phi_{\text{DM}}(r) = \frac{v_0^2}{2} \ln(r^2 + r_0^2)$$

- With these assumptions, the projected second moment  $\mu_2$  of an isotropic model, which is equal to the projected velocity dispersion  $\sigma_p$

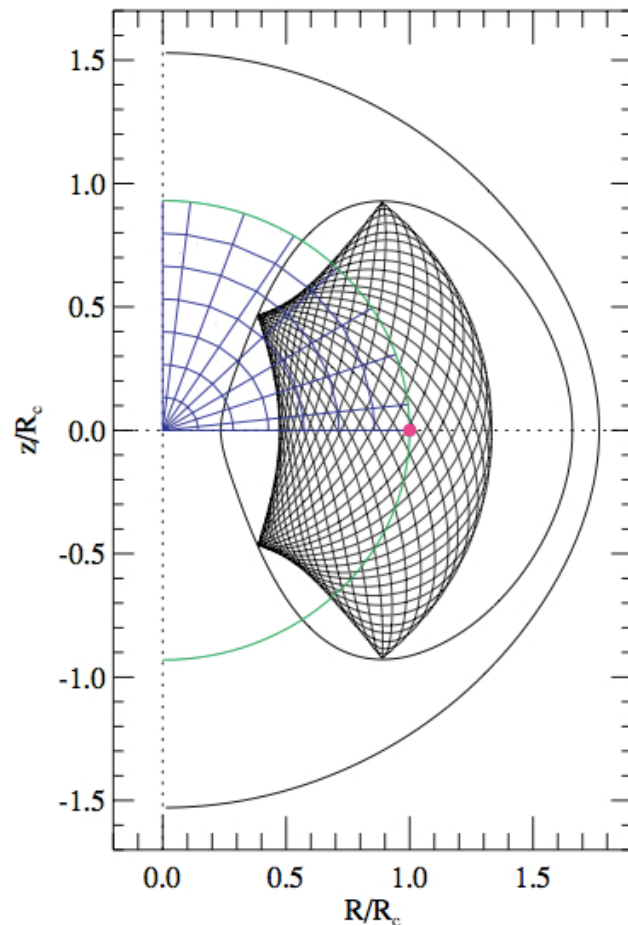
$$\sigma_p^2(R) = \frac{1}{\pi\gamma I(R)} \int_R^{\infty} \left[ \frac{1}{r(r+1)^2} + \frac{v_0^2}{r^2 + r_0^2} \right] \frac{\sqrt{r^2 - R^2}}{(r+1)^3} dr$$

$\rho_{\star}$  and  $\Phi_{\text{DM}}$   The projected velocity dispersion

# Method(3)

~Method to estimate  $(M/L)_{\text{Schw}}$ ~

In this method , the velocity moment is calculated by the higher order moment. (van der Marel et al.(1998))



# Method(4)

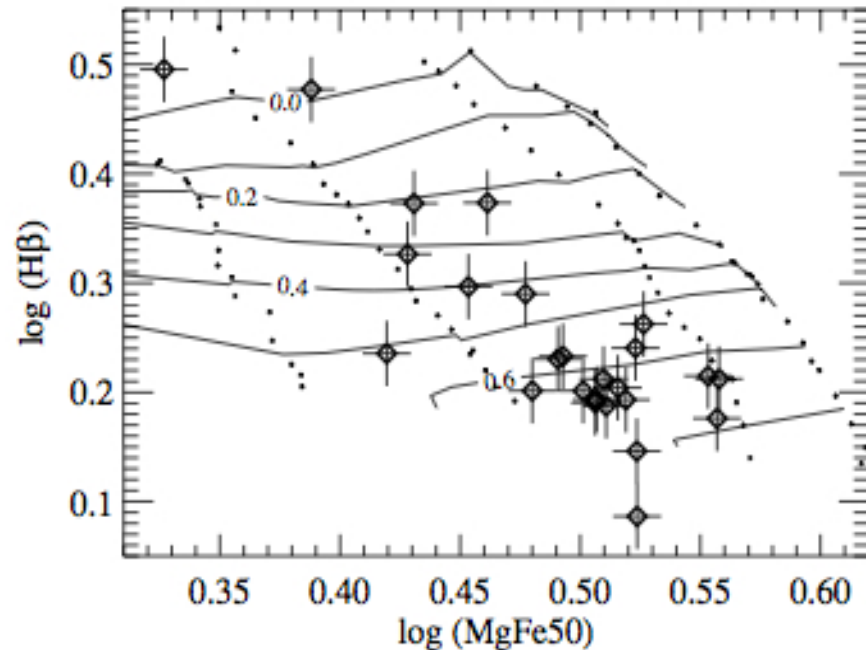
~the tilt of the FP~

- The existence of the FP of the form  $R_e \propto \sigma^\alpha I_e^\beta$ , combined with virial equilibrium assumption  $M \propto \sigma^2 R_e$  and the geometric definition  $L \propto I_e R_e^2$ , yields a prediction for the  $(M/L)_{\text{FP}}$ .
- They adopted an FP determined in the Gunn r band by Jorgensen et al.(1996) from a sample of 225 early-type galaxies in nearby clusters.
- Taking the relation by Jorgensen et al.(1996),

$$R_e \propto \sigma^{1.24 \pm 0.07} I_e^{-0.82 \pm 0.02}$$
$$\left(\frac{M}{L}\right)_{\text{FP}} \propto R^{-0.22 \pm 0.03} \sigma^{0.49 \pm 0.09}$$
$$\left(\frac{M}{L}\right)_{\text{FP}} \propto I_e^{0.02 \pm 0.04} L^{0.31 \pm 0.05}$$

# Method(5)

~Method to estimate  $(M/L)_{\text{pop}}$ ~



- This figure shows that observed values of the line strength index  $\log[\text{MgFe}50]$  versus  $\log[\text{H}\beta]$  for their sample.
- They used the SSP models VZ96 (by Vazdekis et al.(1996) ) and the Salpeter IMF.
- They derived  $(M/L)_{\text{pop}}$  from the SAURON  $\text{Mgb}$  ,  $\text{Fe}5015$  and  $\text{H}\beta$  line-strength indices.

$$[\text{MgFe}50] = 0.5 \times (0.45 \times \text{Mgb} + \text{Fe}5015)$$

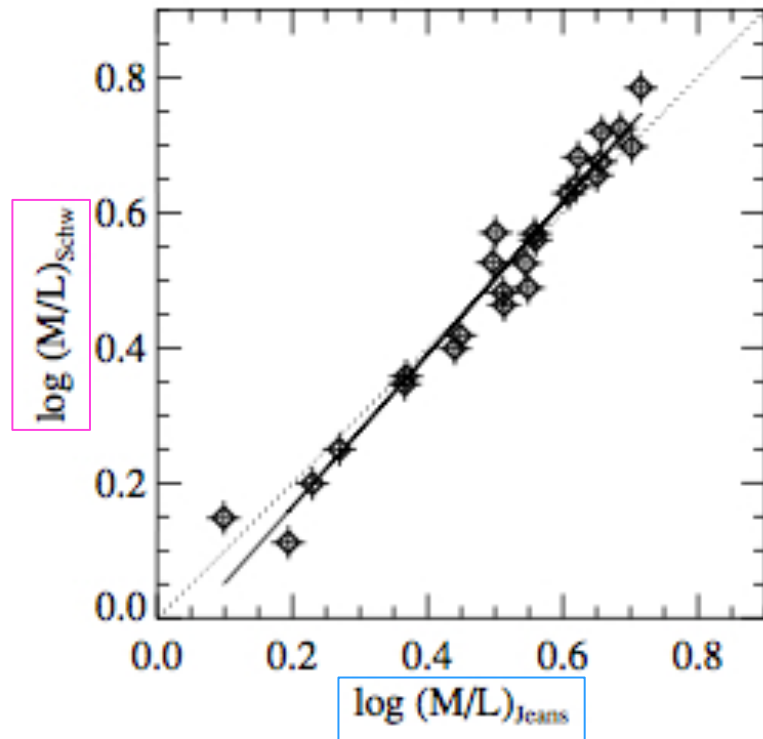
They find that for SSP , the contour levels of constant  $(M/L)_{\text{pop}}$  is essentially a function of  $\text{H}\beta$  alone. In a word a good correlation should exist between  $(M/L)_{\text{pop}}$  and  $\text{H}\beta$  .

# • Results

- (1) Comparing  $(M/L)_{\text{Jeans}}$  and  $(M/L)_{\text{Schw}}$
- (2) Comparison with virial predictions of  $M/L$
- (3) Comparison with stellar population  $(M/L)_{\text{pop}}$
- (4) A second parameter in the  $M/L$  variation

# Result (1)

~Comparing two- and three-integral models~



- The best-fitting correlation shows a small systematic trend  $(M/L) \propto (M/L)_{Jeans}^{1.13 \pm 0.05}$ .
- An error of 6% in the model accuracy is required to explain the observed scatter along the best-fitting relation.
- The galaxy which has the highest M/L tend to show an  $(M/L)_{Schw}$  which is systematically higher than  $(M/L)_{Jeans}$ .

The difference in the M/L is likely due to the fact that the Schwarzschild models use the full information on the LOSVD, while the Jeans models are restricted to the first two moments.

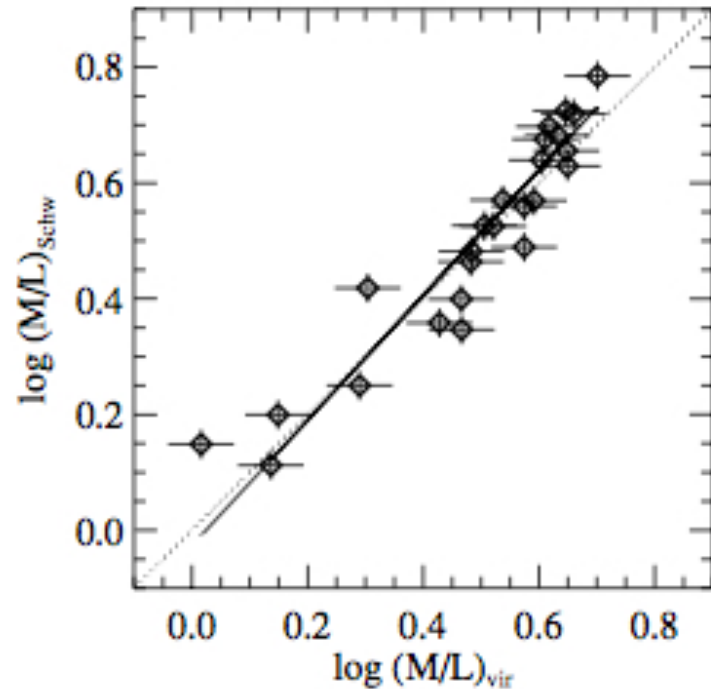


The Schwarzschild model is more general than the Jeans model.



# Result (2)

~Comparison with virial predictions of M/L ~



- This figure shows that comparison between  $(M/L)_{\text{vir}}$  and  $(M/L)_{\text{Schw}}$ .

$$\left(\frac{M}{L}\right)_{\text{vir}} = \frac{\beta R_e \sigma_e^2}{LG}$$

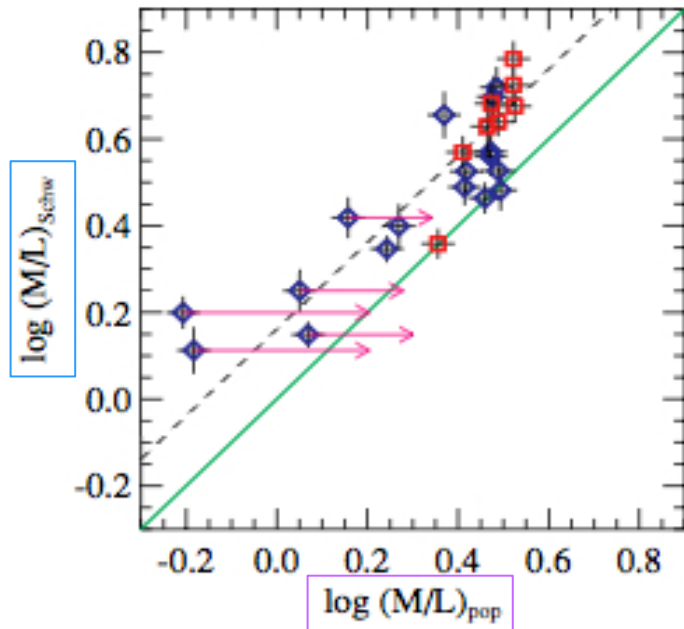
$\beta(n) = 8.87 - 0.831n + 0.0241n^2$ ,  $n$  is Sersic index

- The best-fitting scaling factor is  $\beta = 5.0 \pm 0.1$ .
- They fitted the correlations of  $(M/L)_{\text{vir}}$ , in the I band, with  $\sigma$  and with Luminosity

$$\left(\frac{M}{L}\right)_{\text{vir}} \propto \sigma^{0.82 \pm 0.07}$$
$$\left(\frac{M}{L}\right)_{\text{vir}} \propto L^{0.27 \pm 0.04}$$

# Result (3)

~Comparison with stellar population  $(M/L)_{\text{pop}}$  ~

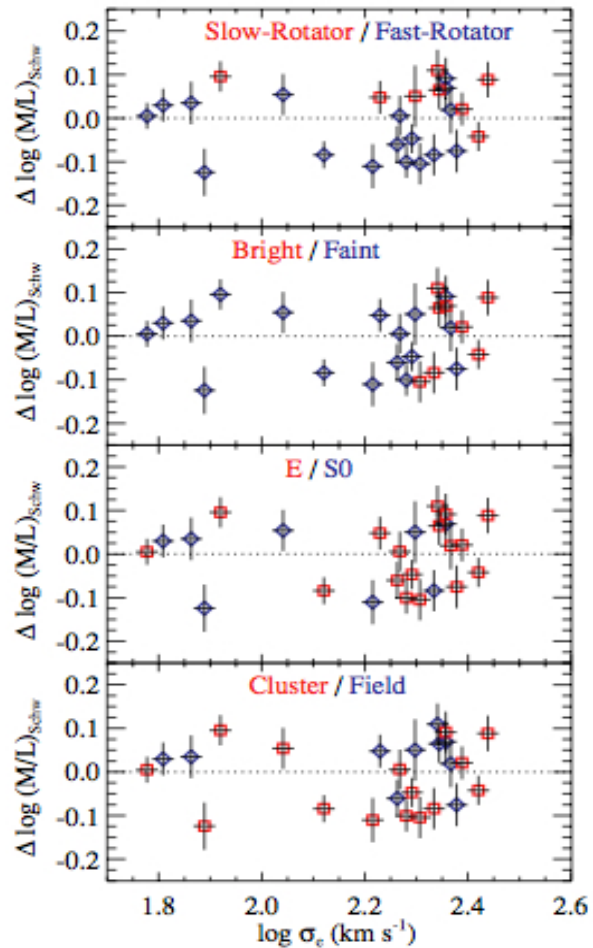


- This figure is  $(M/L)_{\text{Schw}}$  versus a function of  $(M/L)_{\text{pop}}$  using the SSP models of VZ96 and VZ99, with a Kroupa(2001) IMF.
- All galaxies have  $(M/L)_{\text{pop}} \leq (M/L)_{\text{Schw}}$  within the errors, but  $(M/L)_{\text{pop}}$  and  $(M/L)_{\text{Schw}}$  clearly do not follow a one-to-one relation.
- Adopting the Salpeter IMF all values of  $(M/L)_{\text{pop}}$  would increase by  $\Delta \log(M/L) \sim 0.16$ .
- In this case a number of galaxies would have  $(M/L)_{\text{pop}} \geq (M/L)_{\text{Schw}}$ .

The Kroupa IMF constrained the shape below  $1M_{\odot}$  with the result that there are fewer low-mass stars than indicated by the Salpeter IMF.

# Result (4)

~A second parameter in the M/L variations~



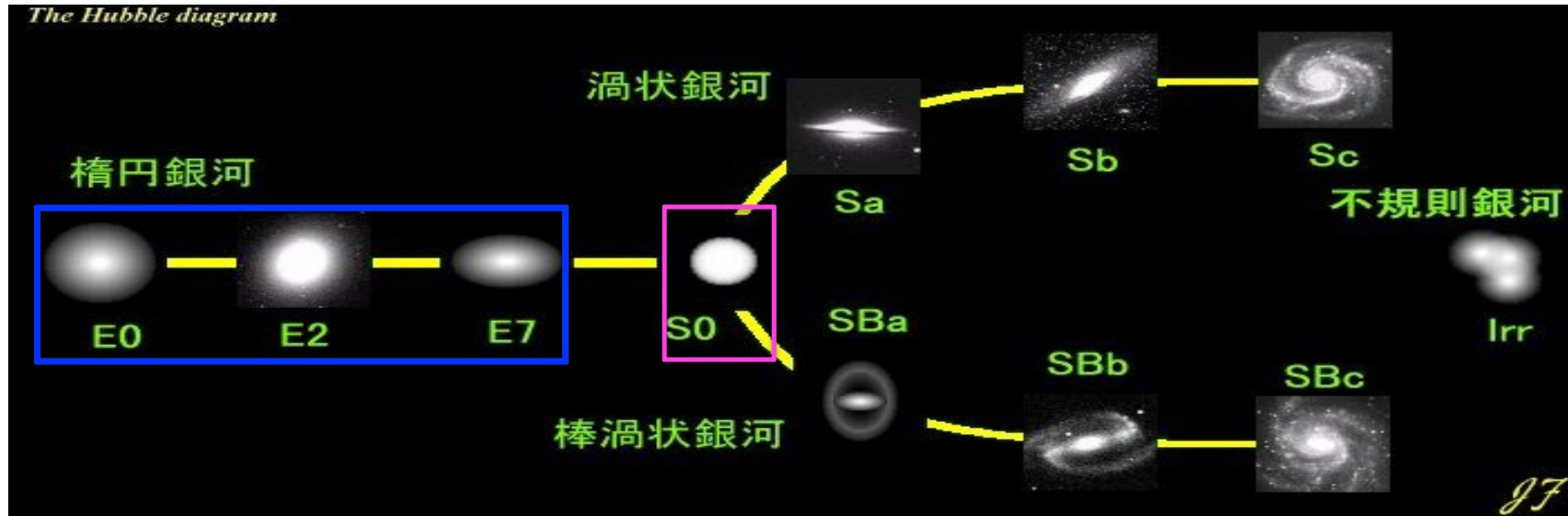
- The first panel shows that there appears to be a tendency for the 'Slow-Rotators' to have a higher M/L than the 'Fast-Rotators', at given  $\sigma_e$ .
- In the second panel, they separate the sample into the galaxies brighter and fainter than the K-band luminosity  $M_K = -24$ .
- The third panel shows that
- The fourth panel shows that the field galaxies have a marginally higher M/L than the cluster galaxies.
- The K-S probability is 2, 32, 74 and 10 % from the top to the bottom panel respectively.

# ▪ Summary

- They find a relation  $(M/L) \propto (M/L)_{\text{vir}}^{1.08 \pm 0.07}$ , which confirms, with small uncertainties, the results from the FP comparisons.
- They find that the M/L generally correlates with the  $(M/L)_{\text{pop}}$ .
- They find some evidence for the variation in M/L to be related to the dynamics of the galaxies.
- In particular the slow-rotating galaxies in their sample, which are more common among the most luminous objects, tend to have a higher M/L at given  $(M/L)_{\text{pop}}$  than the fast-rotating and fainter galaxies.

# Appendix

~Early type galaxies~



## Elliptical galaxy (En)

- Star formation is comparatively inactive and the component is population of an old star.
- Elliptical galaxy is in **a virial equilibrium state** because a velocity dispersion and self-gravity balance.

## Lenticular galaxy (S0)

- The fundamental nature is the same as the nature of an elliptical galaxy.
- However, the region where star formation is comparatively active may exist in lenticular galaxy.

# Appendix

~kolmogorov-Smirnov test (K-S test) ~

- K-S test is a statistical certification to investigate how extent a distribution of an observable quantity and a theoretical quantity are in agreement.
- As practical example , it is confirming the goodness of fit to a gaussian distribution or uniform distribution.
- Making Cumulative-Probability Function (CPF)  $F(x)$  and  $F'(x)$  , the difference  $D$  ( $D = |F(x_{\max}) - F'(x'_{\max})|$ ) in the place  $x_{\max}$  where the distance of CPF becomes the maximum.
- Significant probability

$$Prob(D\sqrt{N} > z) = 2 \sum_{j=1}^{\infty} (-1)^{j-1} \exp(-2j^2 z^2)$$