

Section 2.

Stellar structure and properties (I)

2.1 Hydrostatic equilibrium

2.2 Nuclear burning

Goals of this lecture

- **Standard properties of stars**
 - **Stellar structure and properties**
 - **Stellar evolution**
- **Origin of the elements in the Universe**
 - **Nucleosynthesis in stars and supernovae**
 - **Explosion mechanism of supernovae**
- **Topics in time-domain astronomy**
 - **Radiation from explosive phenomena**
 - **Multi-messenger astronomy**

Our sun

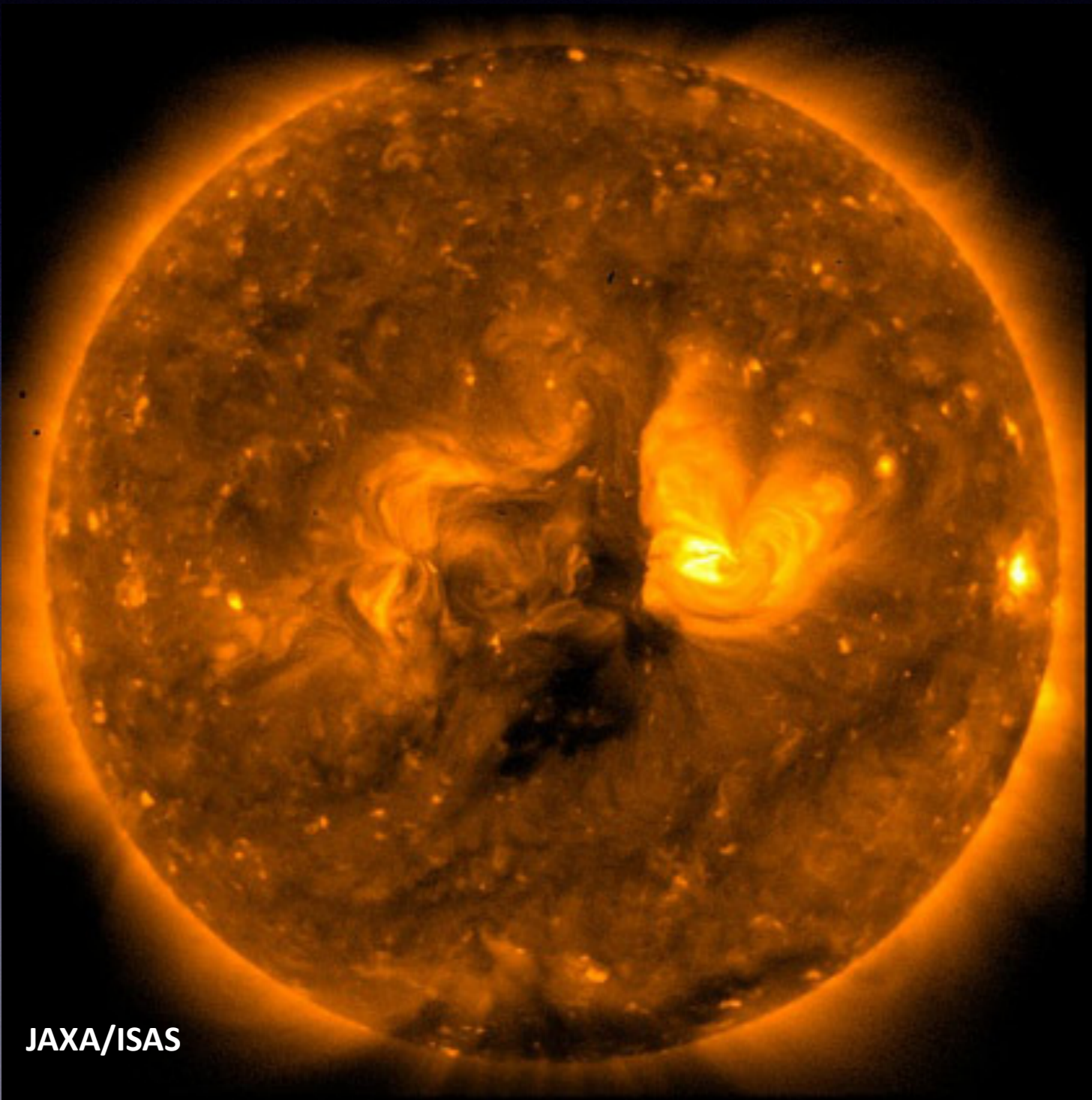
$$L = 4 \times 10^{33} \text{ erg/s} = 4 \times 10^{26} \text{ J/s (W)}$$

Electronic power consumption in Japan

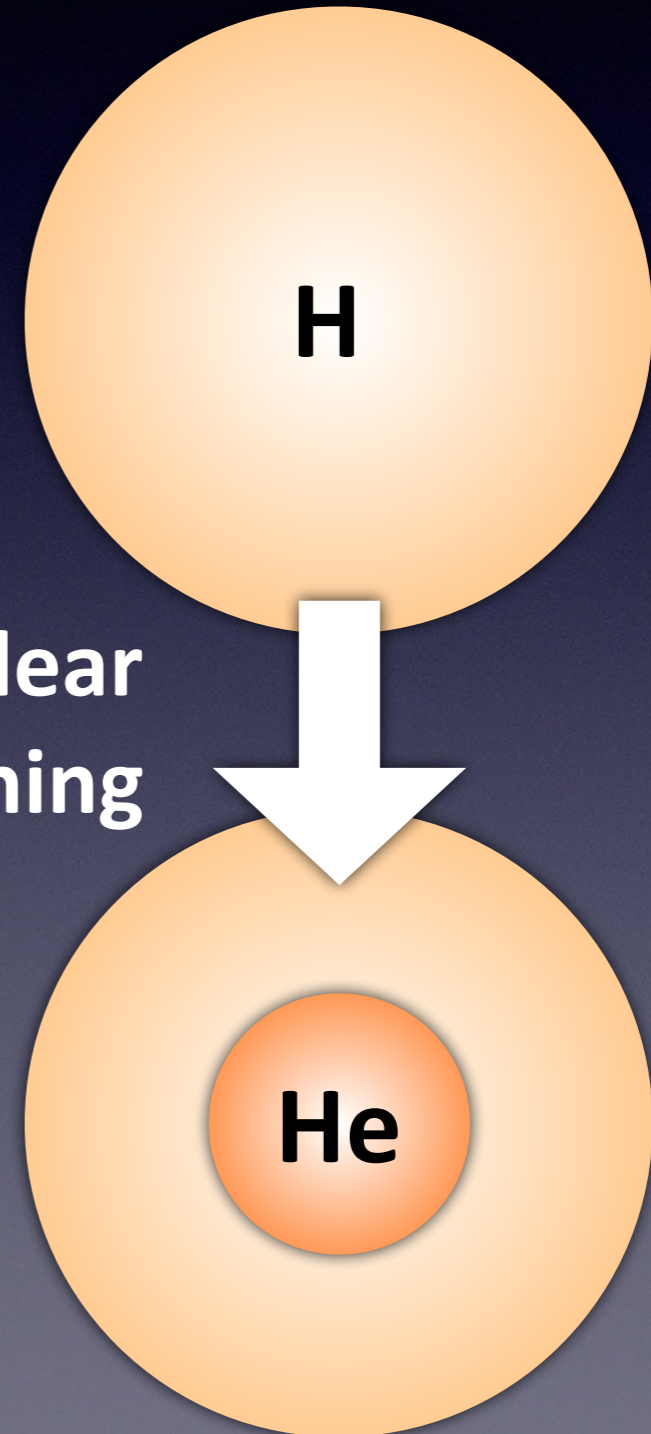
$1.5 \times 10^{19} \text{ J / year}$

==> Japanese power consumption for $2 \times 10^7 \text{ yr}$

= solar radiation in 1 second

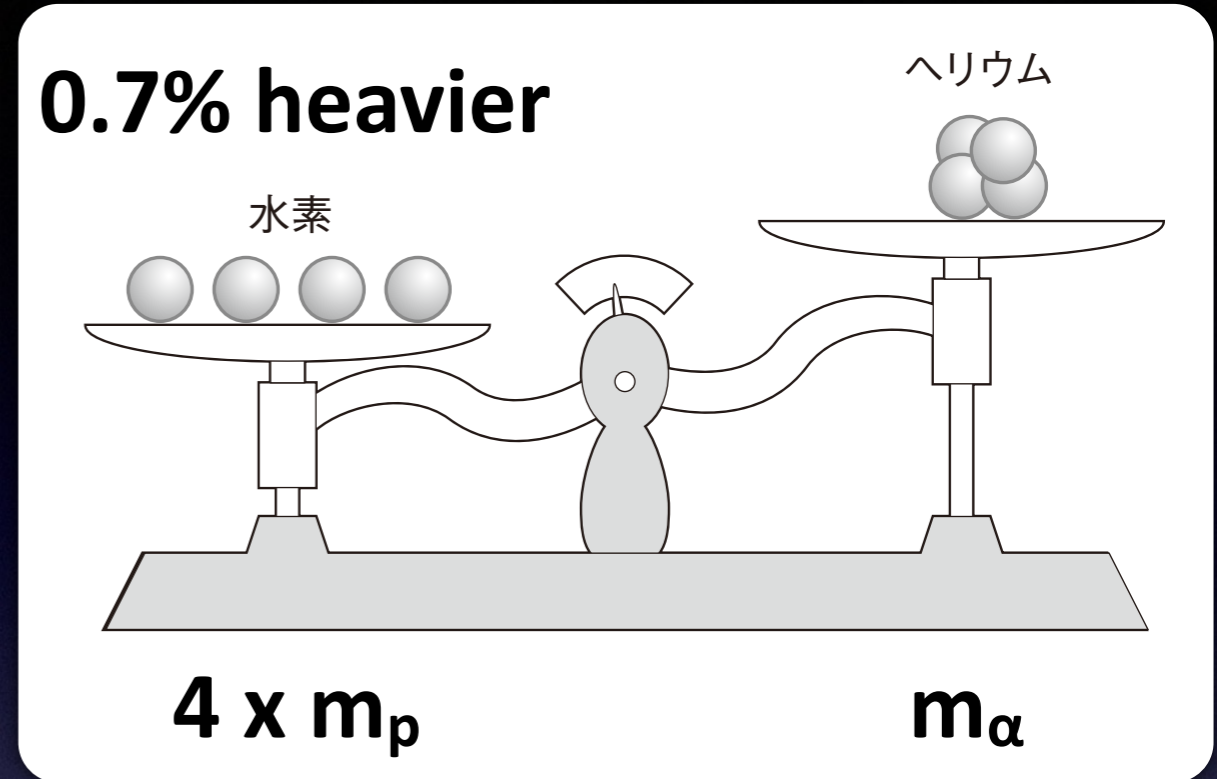


Nuclear
burning





Energy source: $E = mc^2$



Q1: How much energy is released for one nucleon? (核子あたり)

$$E = \Delta mc^2$$

Solar mass : 2×10^{33} g

Q2: How much energy does the Sun can produce?

(assume 10% of solar mass can be used for nuclear burning)

Q3: How many years the sun can keep shining?

$$L = 4 \times 10^{33} \text{ erg/s}$$

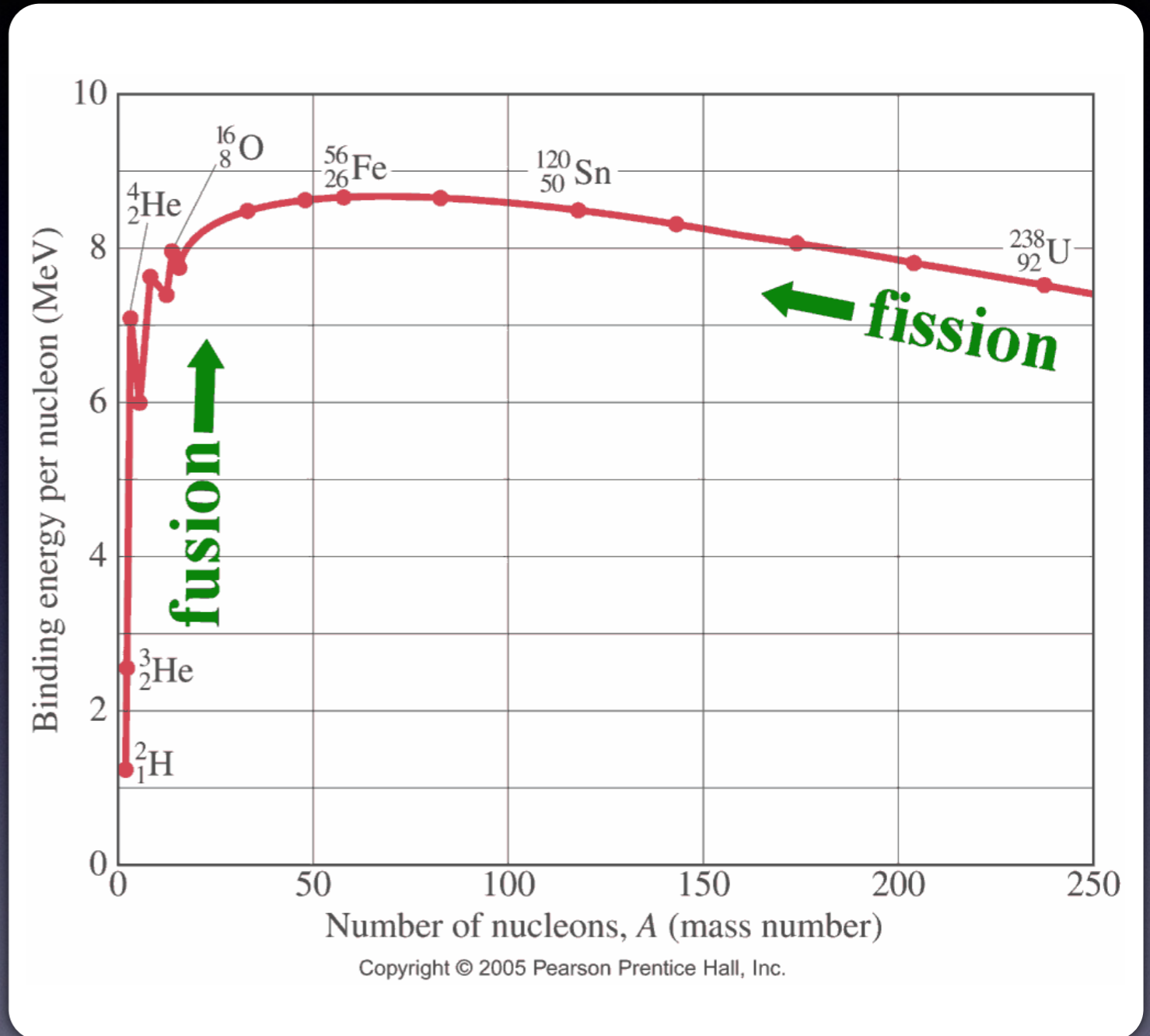
$$1 \text{ yr} \sim 3 \times 10^7 \text{ sec}$$

Binding energy of nuclei

$$E_b = \frac{[Nm_N + Zm_p - m_i] c^2}{P + n \quad \text{Nuclei}}$$

Higher binding energy
= strongly “bound”
= more stable
= “lighter”

Fe is the most stable nucleus





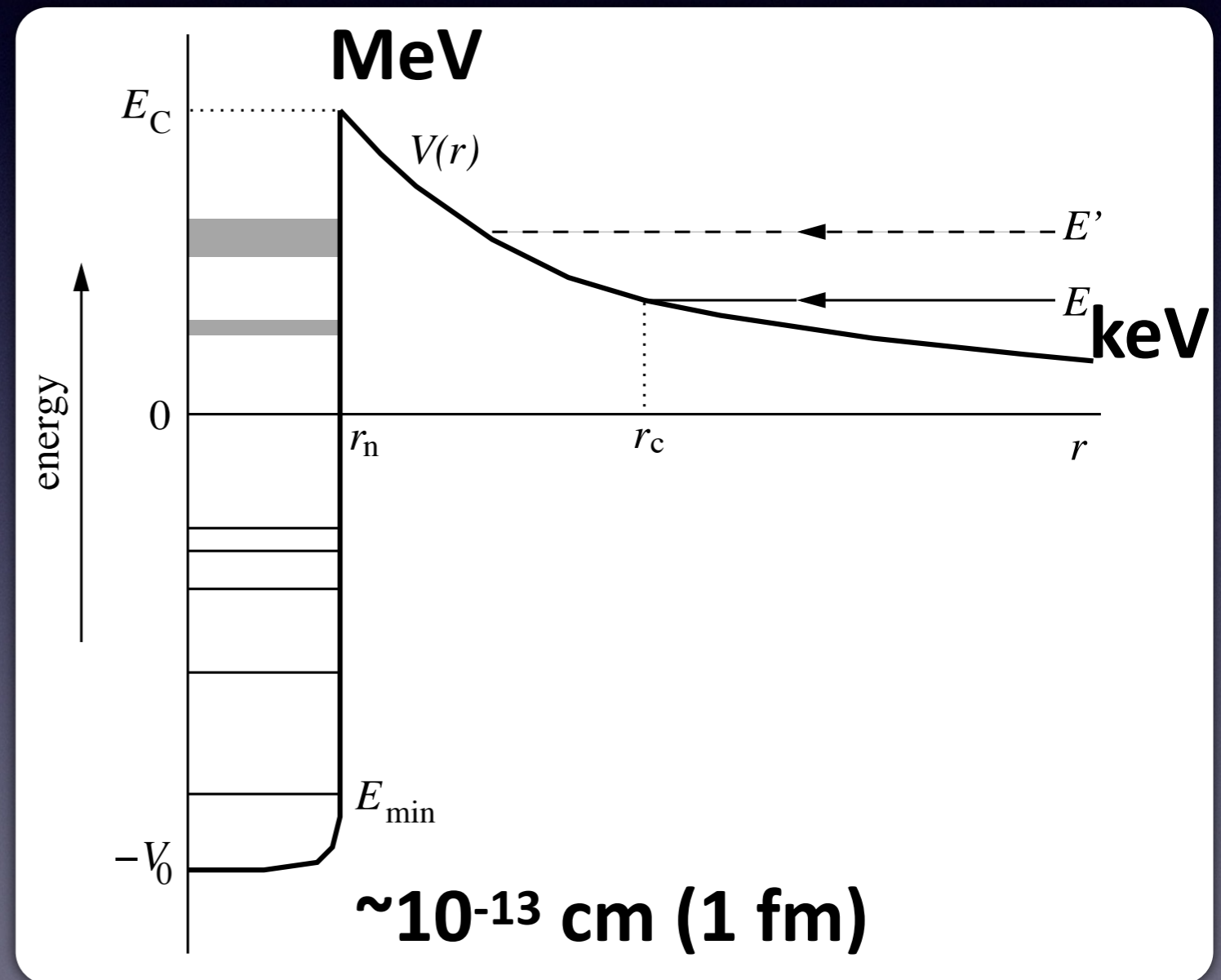
**What is going on at the center of the star?
How does nuclear burning occurs?**

Nuclear burning

Coulomb barrier $E \sim (Z_1 Z_2 e^2)/r \sim 10^6 \text{ eV (MeV)}$

Typical energy of the gas $E \sim kT \sim 10^3 \text{ eV (keV)} \ll 10^7 \text{ K}$

=> Tunnel effects



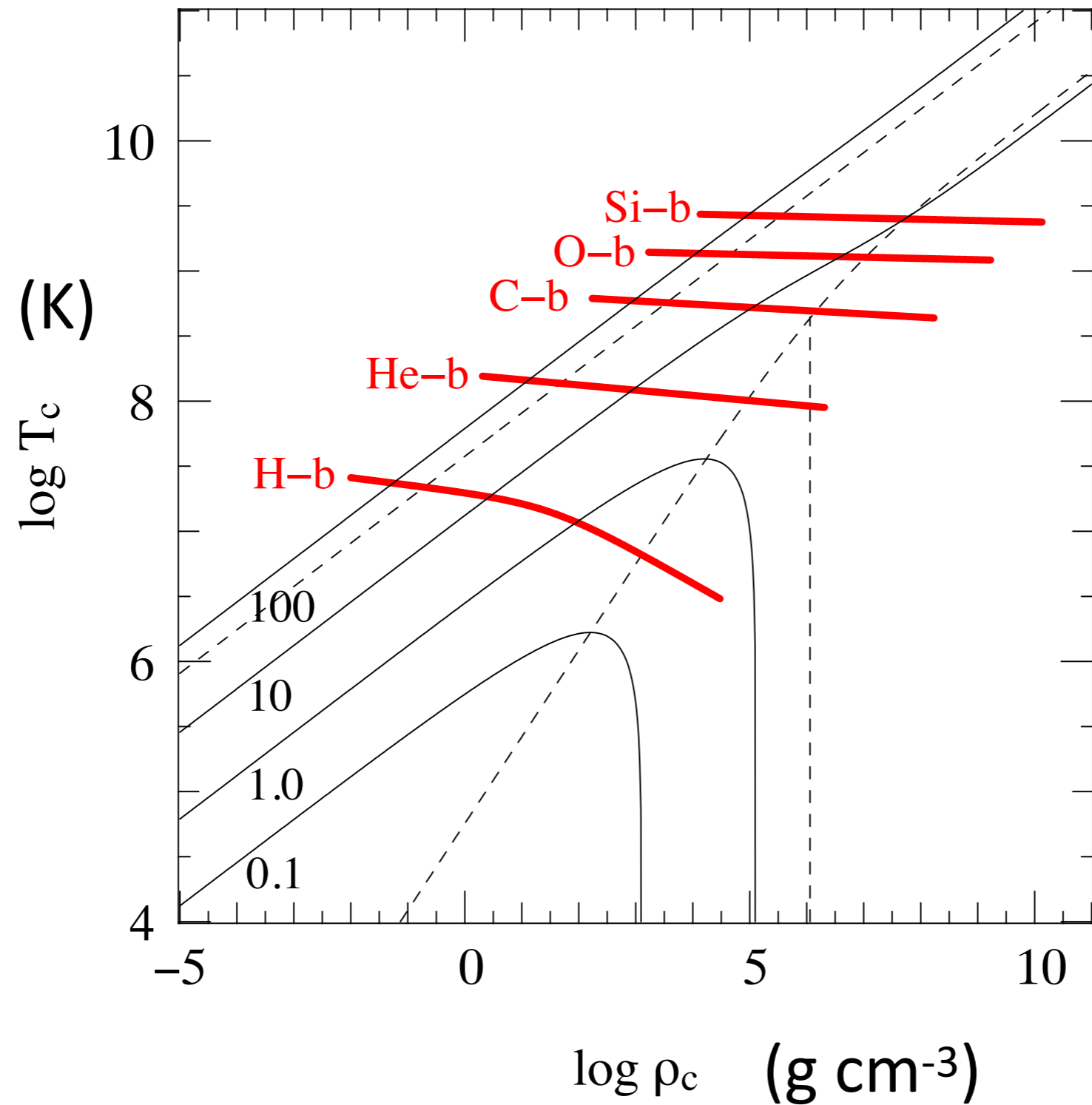
Condition of H-burning

Fusion
reactor

$\sim 10^8$ K

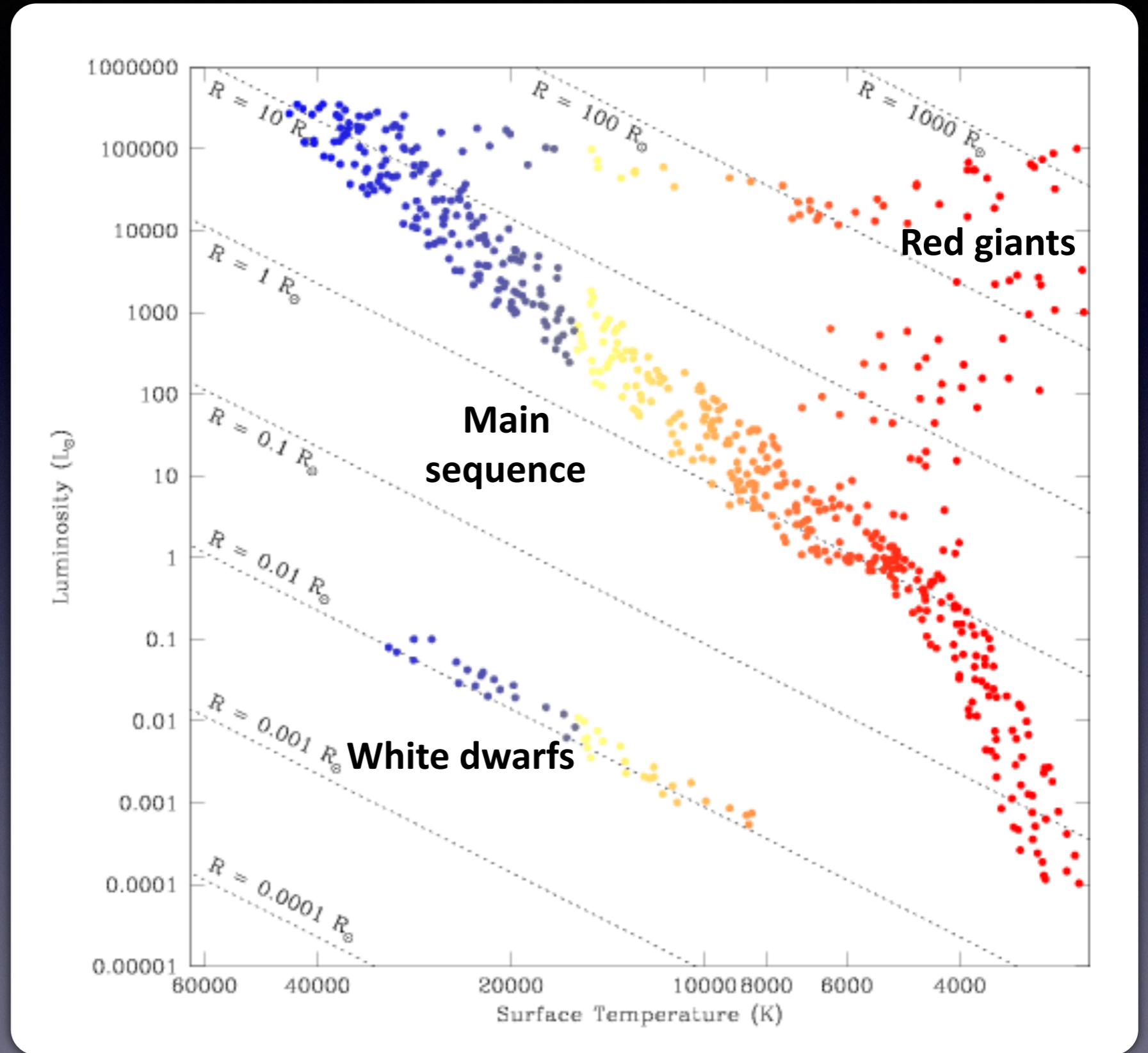


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Hertzsprung-Russel diagram

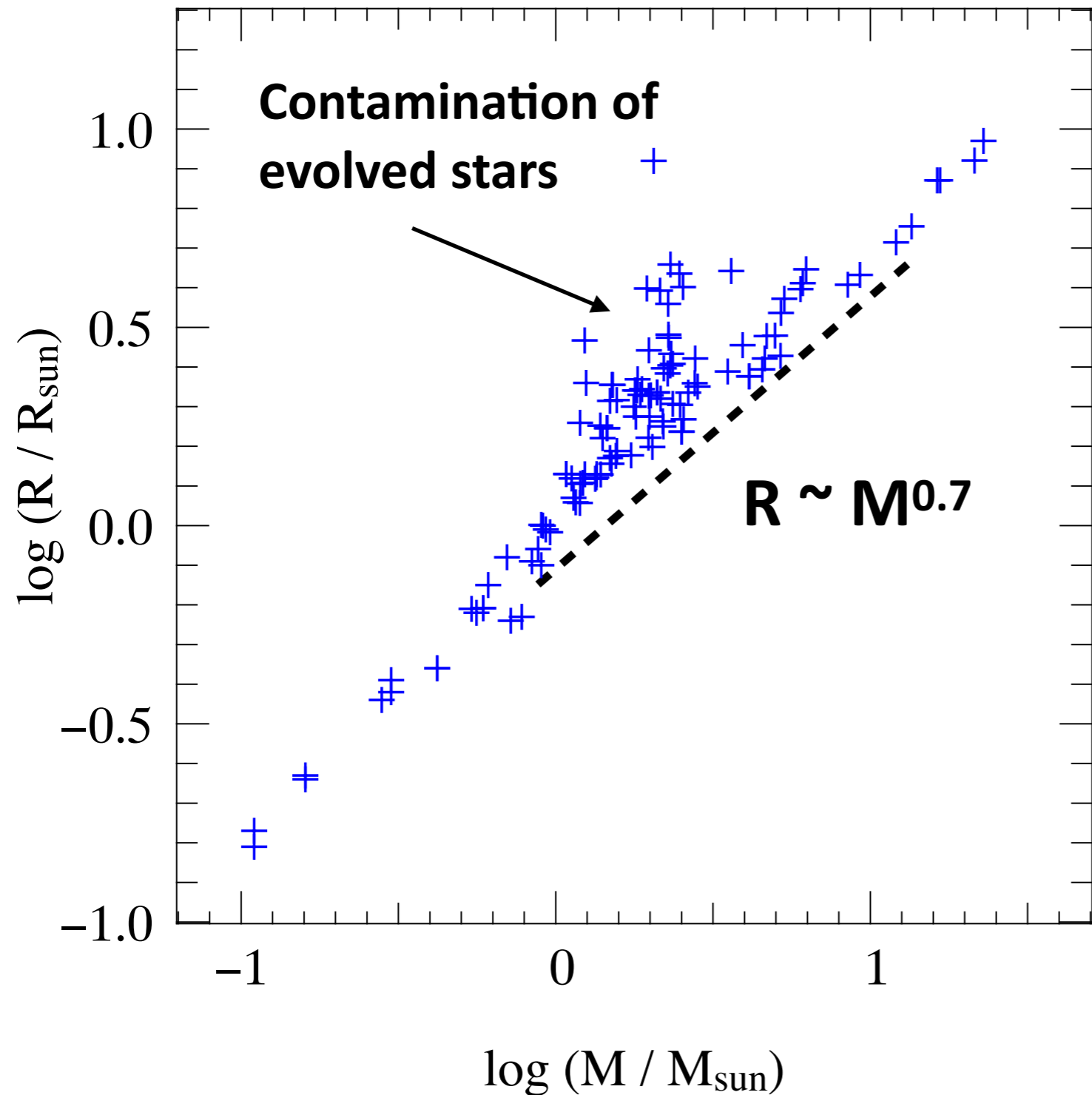
Luminosity



Temperature (K)



Mass - radius relation for the main sequence



**Outcome of
the central property
of the star**

Summary: Stellar structure and properties (I)

- Energy source of the stars
 - Nuclear burning
 - $E = mc^2$
- Stellar structure
 - Hydrostatic Equilibrium
 - Central temperature of the stars $T \sim 10^7$ K
 - Require tunnel effects for nuclear burning
- Stellar properties
 - Almost constant central $T \Rightarrow R \sim M$
 - Observed mass-radius relation ($R \sim M^{0.7}$)