

Section 3.

Stellar structure and properties (II)

3.1 Luminosity of the stars

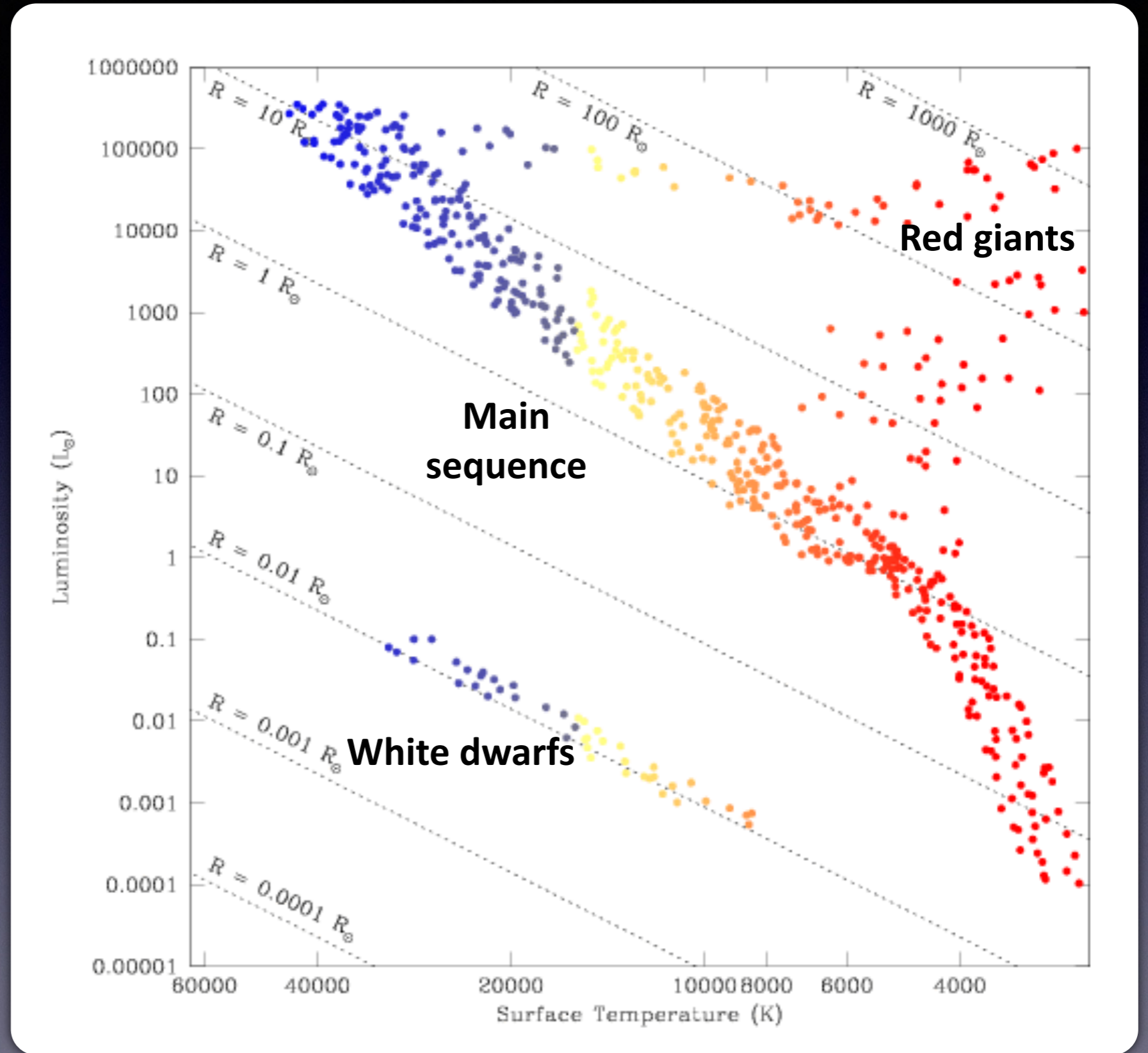
3.2 Opacities in the stars

Let's understand these questions with the words of physics

- Why are stars so luminous?
- Why do stars show $L \sim M^4$?
- Why do stars evolve?
- Why does the destiny of stars depend on the mass?
- Why do some stars explode?
- Why don't normal star explode?
- Why does stellar core collapses?
- Why is the energy of supernova so huge?
- ...

Hertzsprung-Russel diagram

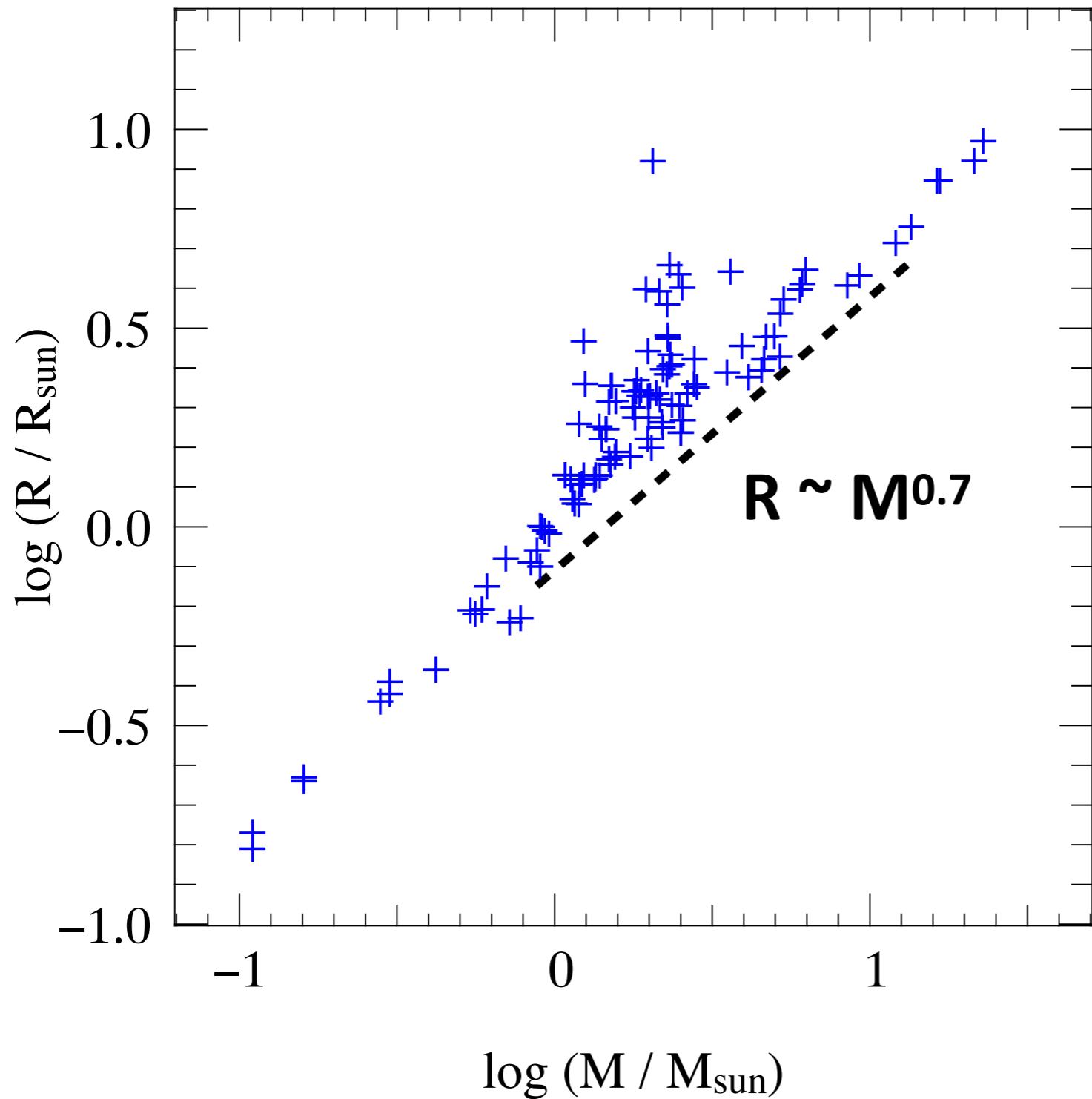
Luminosity



Temperature (K)

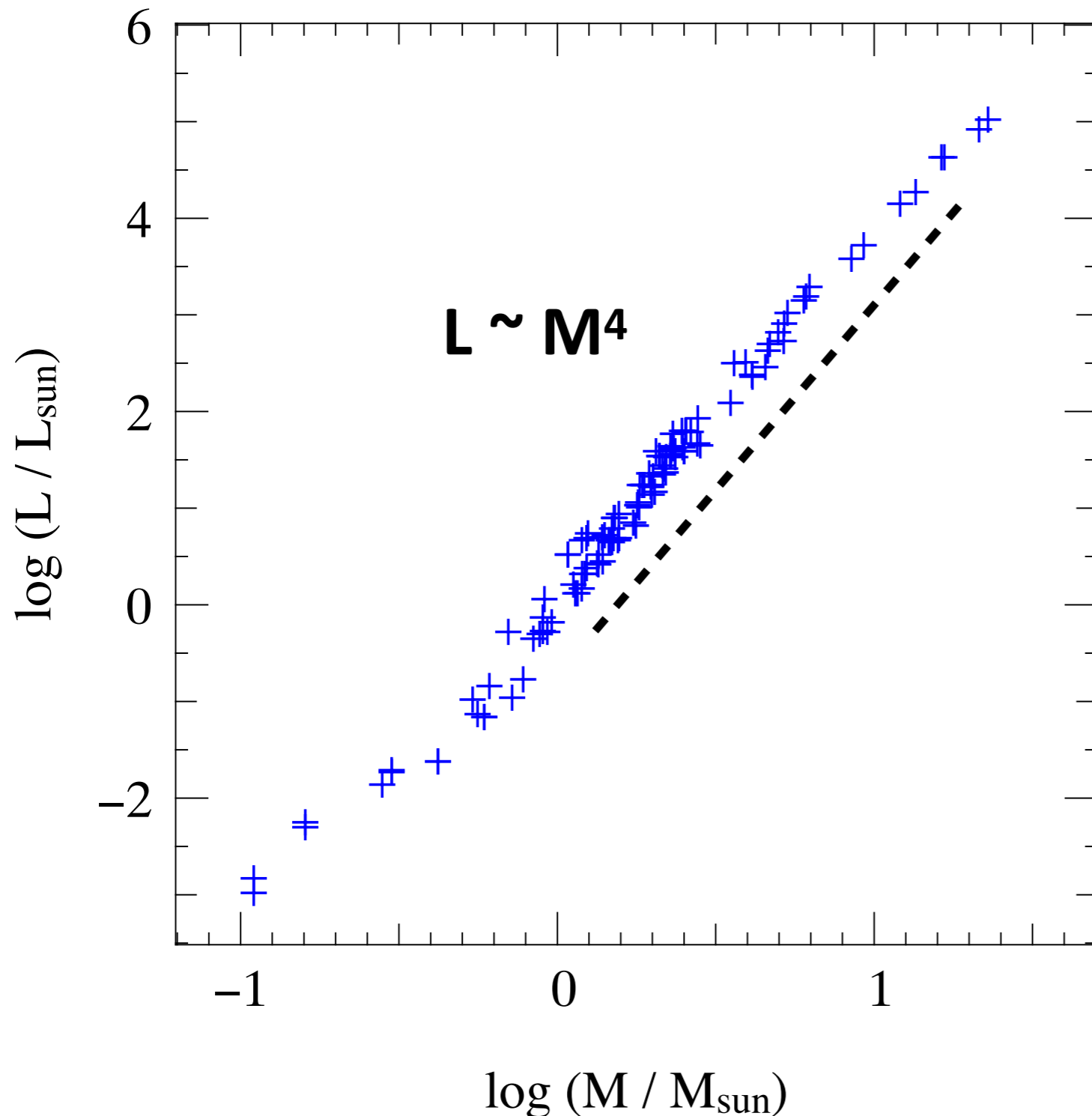


Mass - radius relation for the main sequence



**Outcome of
the central property
of the star**

Mass - luminosity relation of the main sequence stars



Star with $M = 10 M_{\text{sun}}$
 $\Rightarrow L \sim 10^4 L_{\text{sun}}$
 \Rightarrow Lifetime
 $\sim 1/10^3$ of the Sun
 $\sim 10^{10}$ yr (100億年)/ 10^3
 $\sim 10^7$ yr (1000万年)

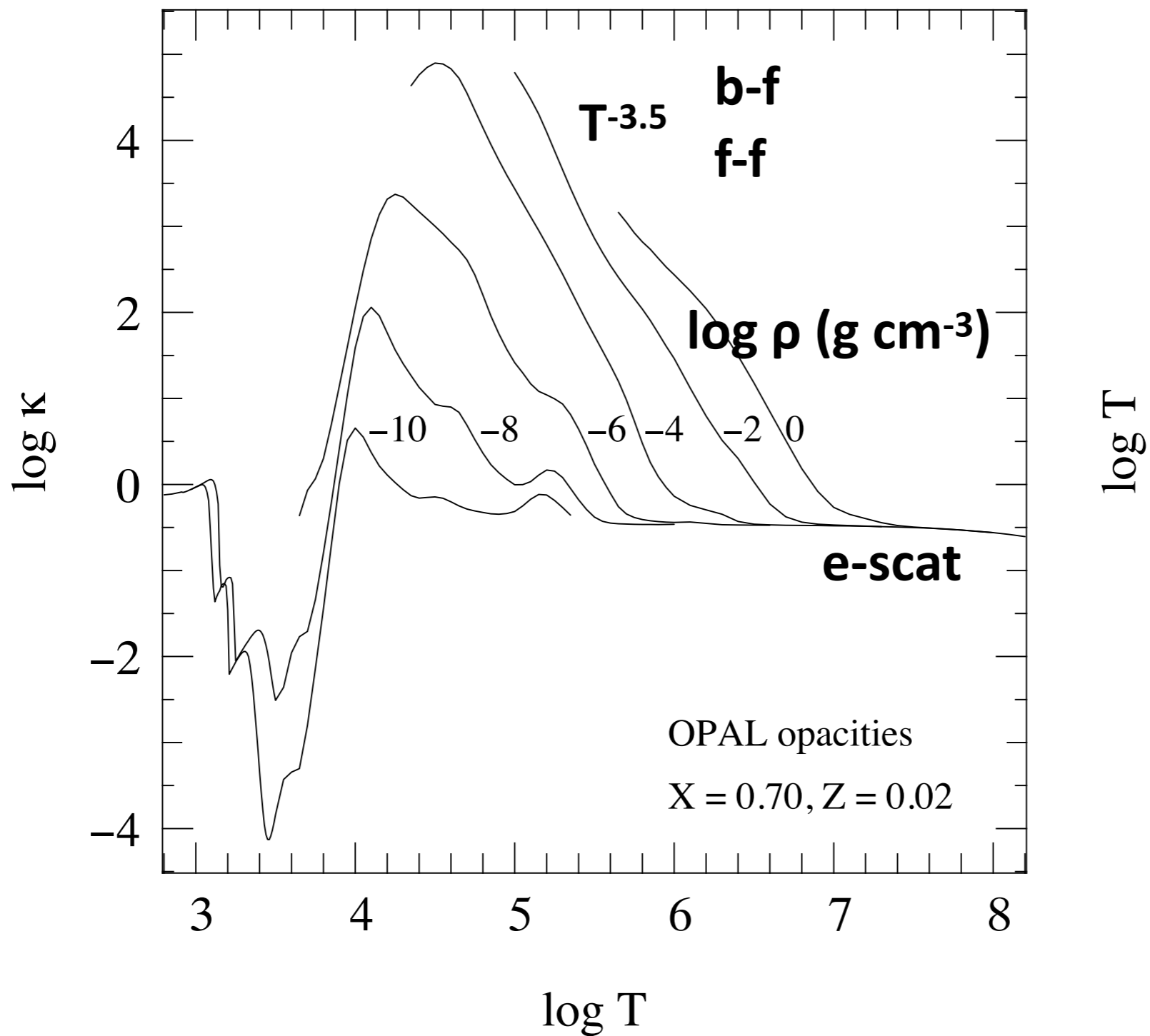
**More massive stars
have shorter lifetime**



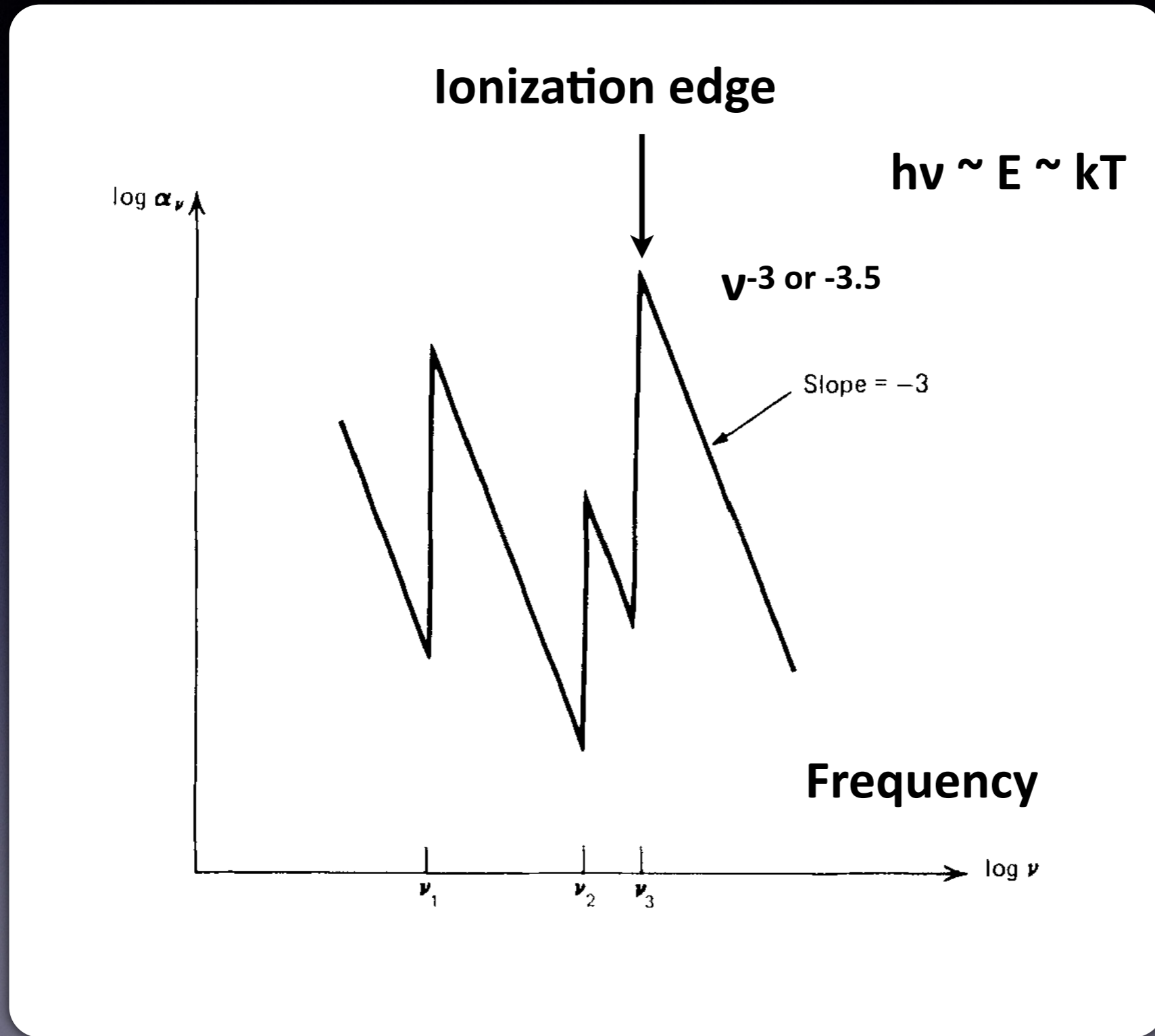
Why do stars show $L \sim M^4$?

Why do more massive stars have higher temperature?

Opacity inside the stars



Bound-free opacity



Assignment 1

Derive that the dependence of free-free opacity in stellar interior can be approximated as $\kappa \propto \rho T^{-3.5}$

Hint: In equilibrium, the rate for free-free absorption matches with that of free-free emission (thermal bremsstrahlung), i.e. $j_\nu = \alpha_\nu B_\nu(T)$

* Kirchhoff's law

レポート課題 1

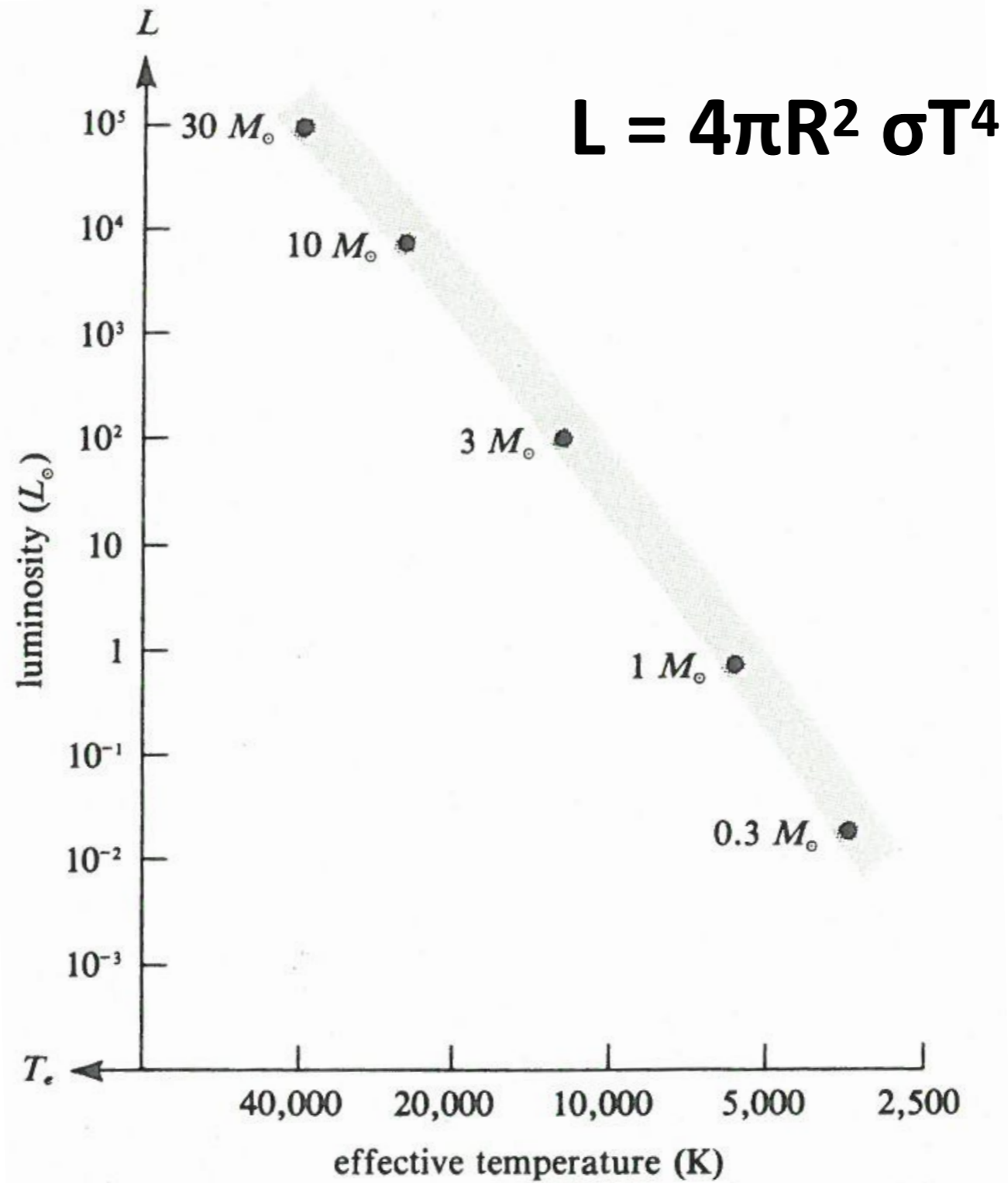
恒星内部における自由-自由吸収の密度・温度依存性が近似的に次のように表せられることを示せ $\kappa \propto \rho T^{-3.5}$

ヒント：平衡状態では自由-自由吸収のrateと自由-自由放射 (熱的制動放射)のrateはつり合う $j_\nu = \alpha_\nu B_\nu(T)$

* キルヒホッフの法則

Hertzsprung-Russel diagram

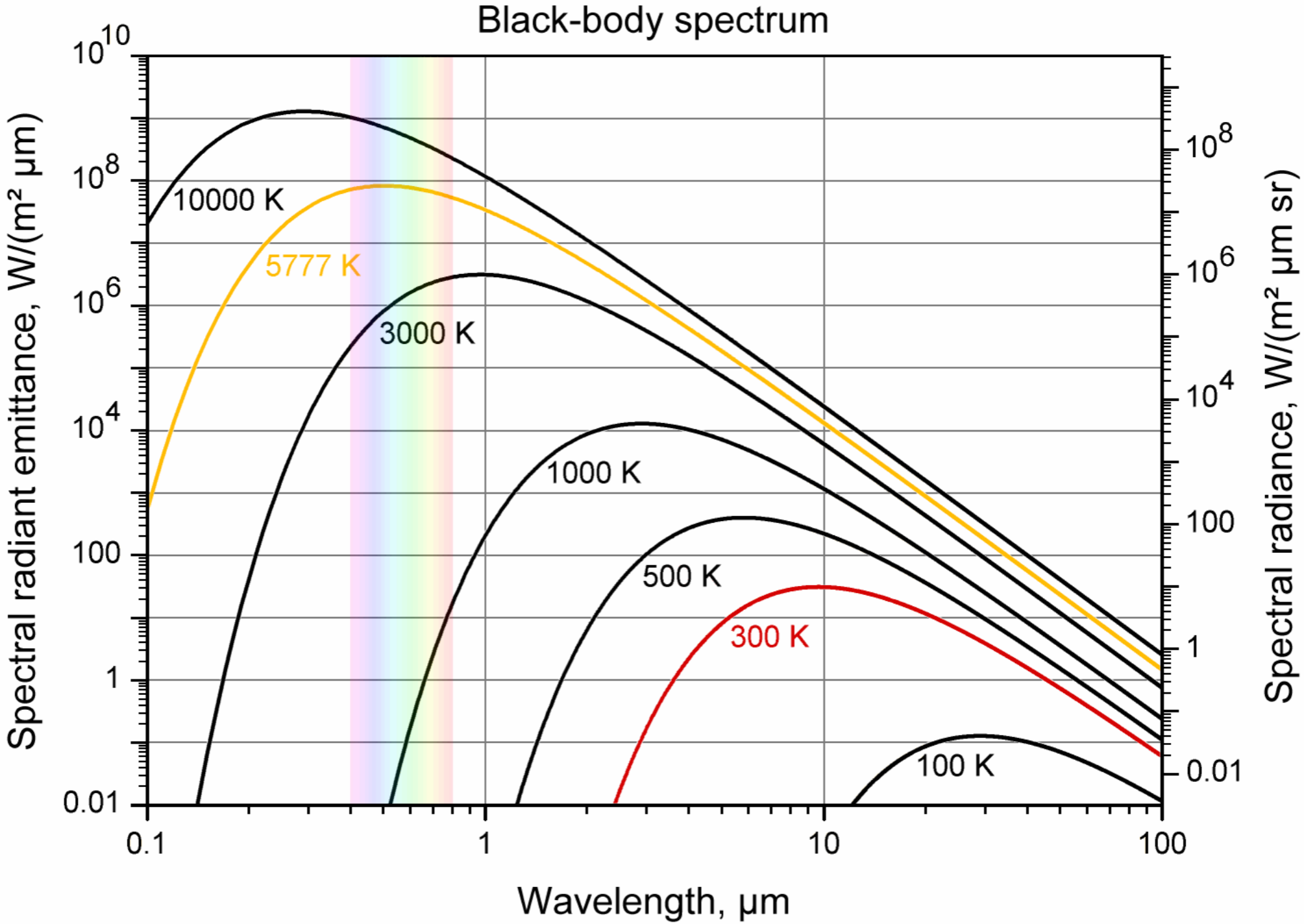
L



T (K)

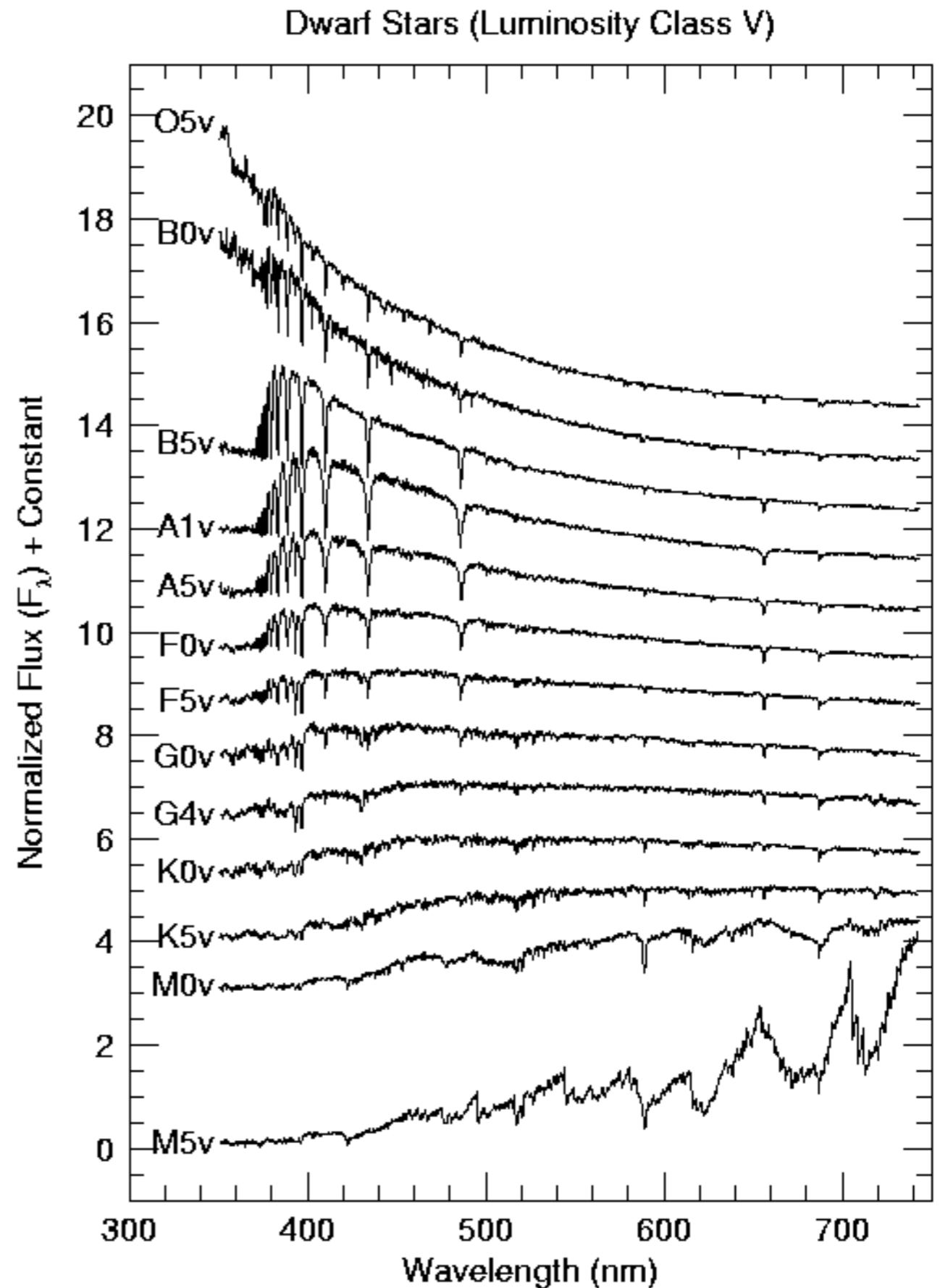


Blackbody radiation



Stellar spectrum

Type	M (Msun)
O	20-60
B	3-18
A	2-3
F	1.1-1.6
G	0.9-1.05
K	0.6-0.8
M	0.08-0.5



Applications to galaxy studies

Spiral galaxy

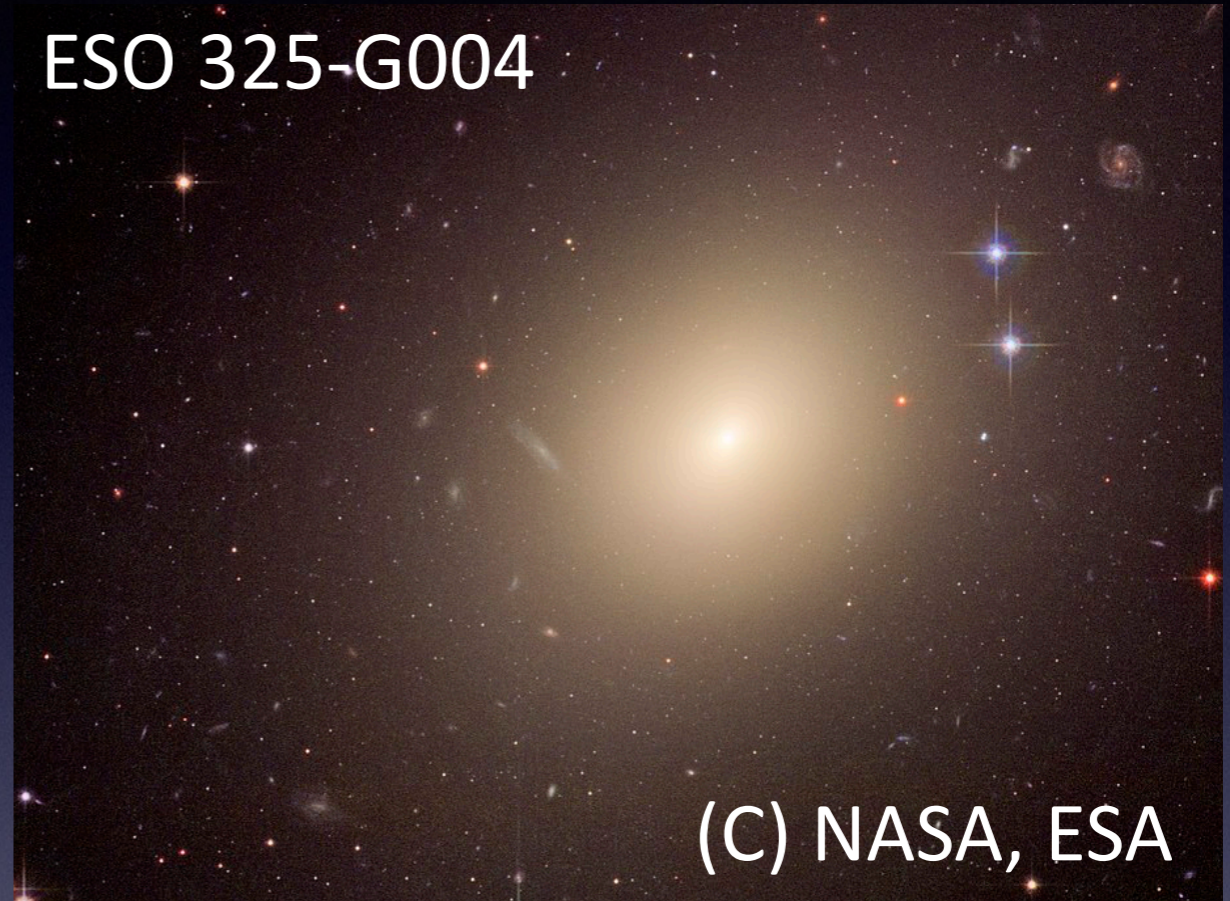
M101



- Star forming
- More "young" stars
- More massive stars
- Blue (high T radiation)

Elliptical galaxy

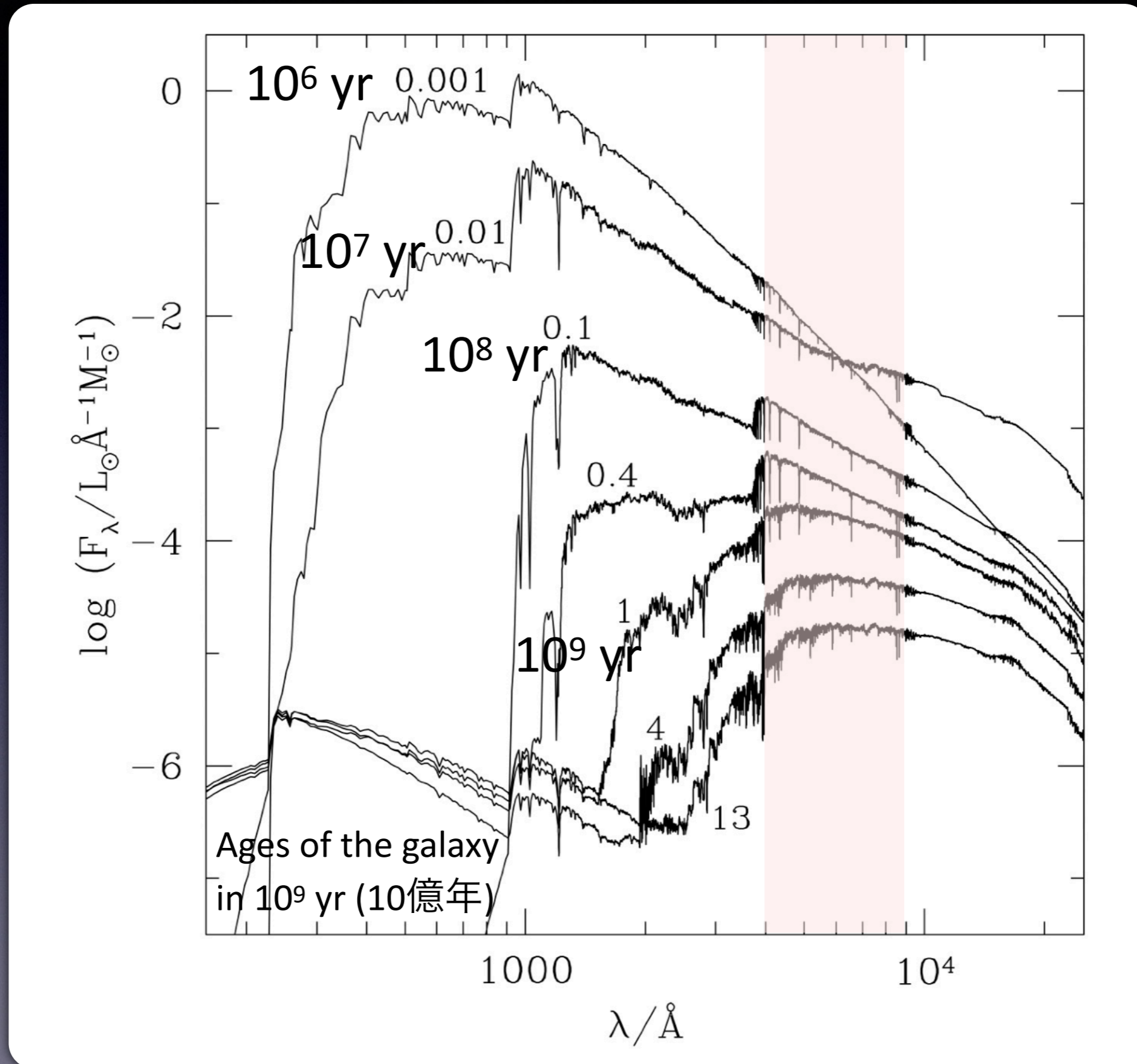
ESO 325-G004



- No star formation
- Old stars
- Less massive stars
- Red (low T radiation)

Spectral models for galaxies

Bruzual & Charlot 2003



Summary: Stellar structure and properties (I)

- Opacities in the stars
 - Thomson scattering
 - free-free and bound-free absorption
- Luminosity of the stars
 - $L \sim E/t_{\text{esc}}$, where $t_{\text{esc}} \sim (R/c) \tau$ ($\tau = \kappa \rho R$)
 - $L \sim M^{3-5}$
- Stellar properties
 - More massive stars have
 - Higher luminosity $L \sim M^4$ (shorter lifetime $t \sim M^{-3}$)
 - Higher temperature $T_{\text{eff}} \sim M^{0.5}$
 - Foundation to determine the galaxy spectra

Thermodynamics

Electromagnetism

**Classical
mechanics**

**Statistical
mechanics**

Astrophysics

Hydrodynamics

**Quantum
mechanics**

Relativity

Nuclear physics