

Section 5.

Stellar evolution (II)

5.1 Equation of state

5.2 Evolutionary track

Let's understand these questions with the words of physics

- Why are stars so luminous?
- Why do stars show $L \sim M^4$?
- Why do stars evolve?
- Why does the destiny of stars depend on the mass?
- Why do some stars explode?
- Why don't normal star explode?
- Why does stellar core collapses?
- Why is the energy of supernova so huge?
- ...

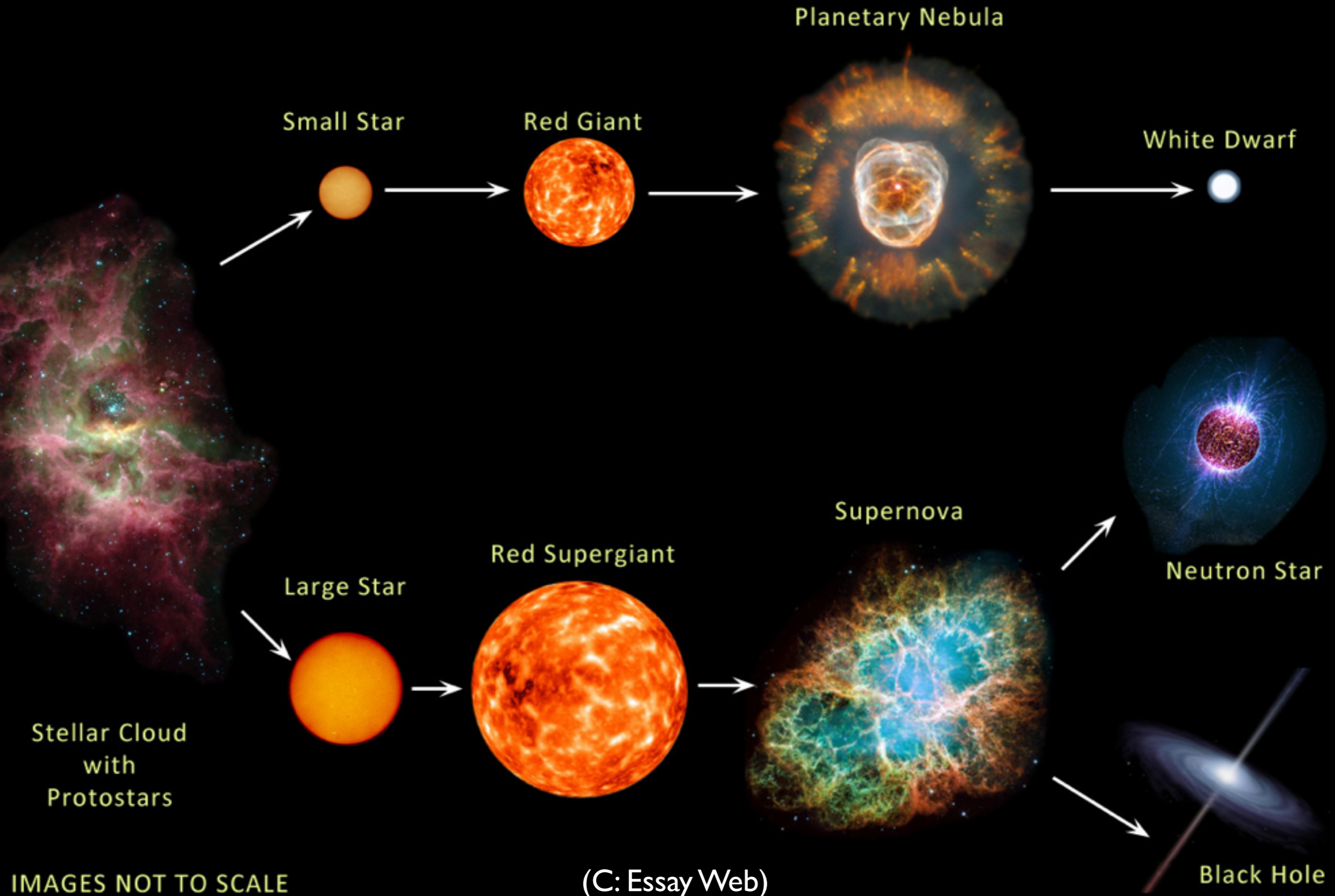
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Stellar life



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(C: Essay Web)



Why does the destiny of the stars depend on the mass?

Microscopic properties of the gas play important roles

Assignment 2

2a. Derive pressure of ideal gas from the Maxwell distribution

**2b. Derive pressure of degenerate electrons
(both for non-relativistic case and relativistic case)**

2c. Derive radiation pressure from Planck function

2d. Draw the regions where

- ideal gas pressure**
- degenerate pressure of non-relativistic electrons**
- degenerate pressure of relativistic electrons**
- radiation pressure**

become dominant in the ρ - T diagram.

レポート課題 2

2a. マクスウェル分布から
理想気体の圧力の式を導け

2b. 電子が非相対論的、超相対論的などの
縮退圧の式を導き、実際に数字を入れて計算せよ

2c. プランク関数から輻射圧の式を導け

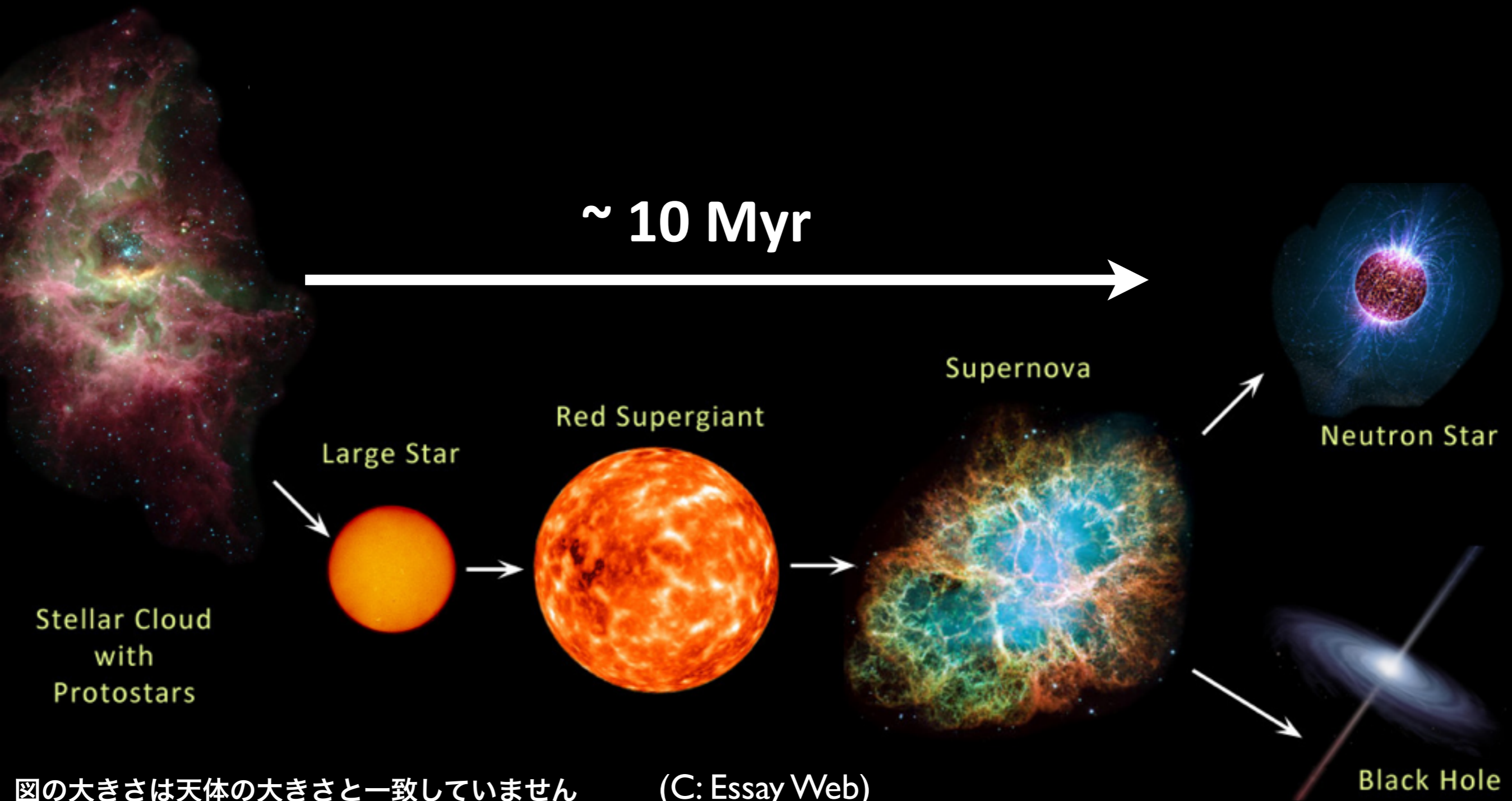
2d. 密度 - 温度平面で

- 理想気体のガス圧
- 電子の縮退圧 (非相対論的)
- 電子の縮退圧 (超相対論的)
- 輻射圧

がそれぞれ支配的になる境界を求め、図示せよ

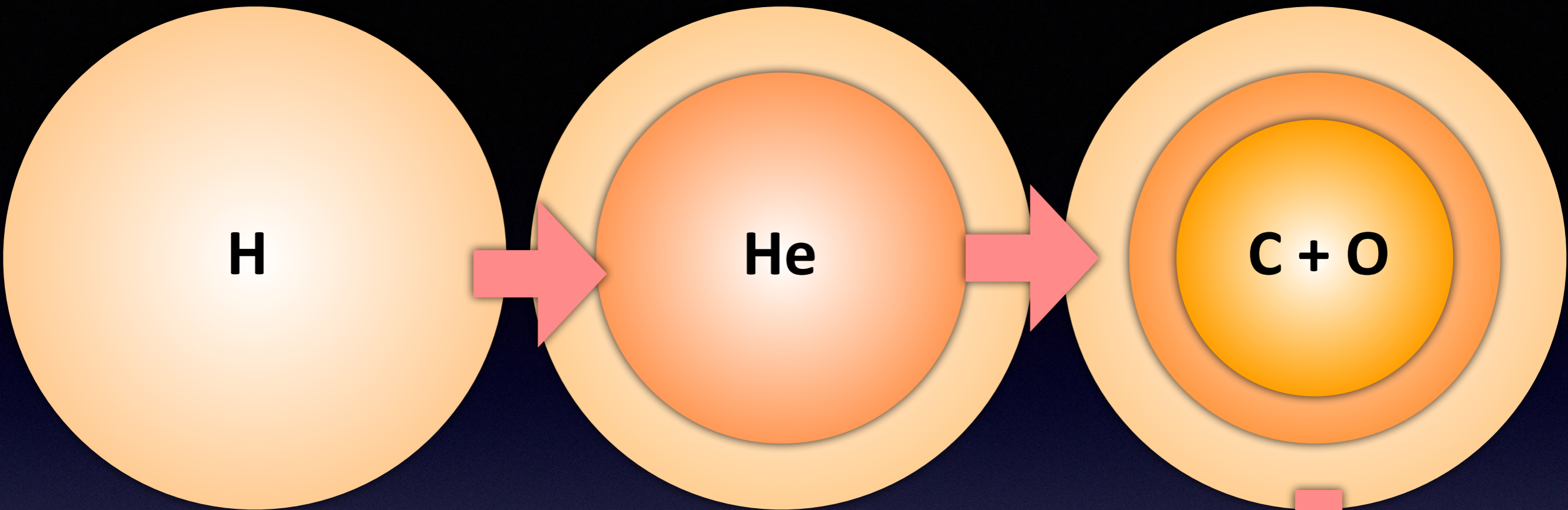
1. Massive stars

$M > 10 M_{\text{sun}}$

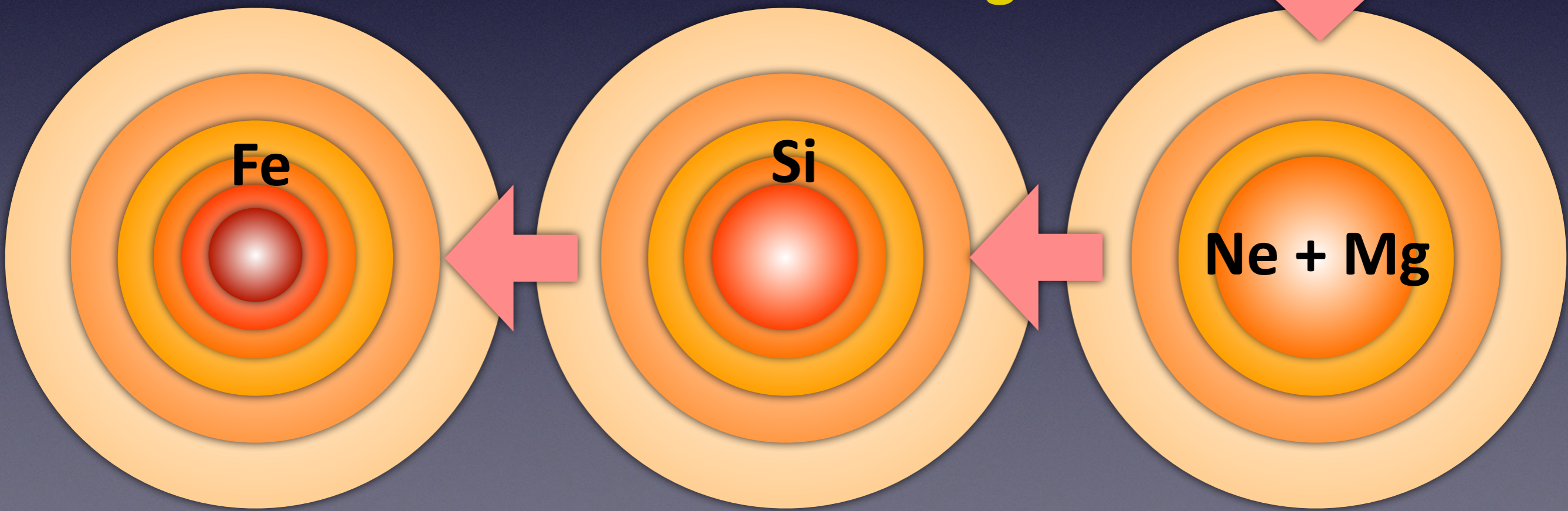


図の大きさは天体の大きさと一致していません

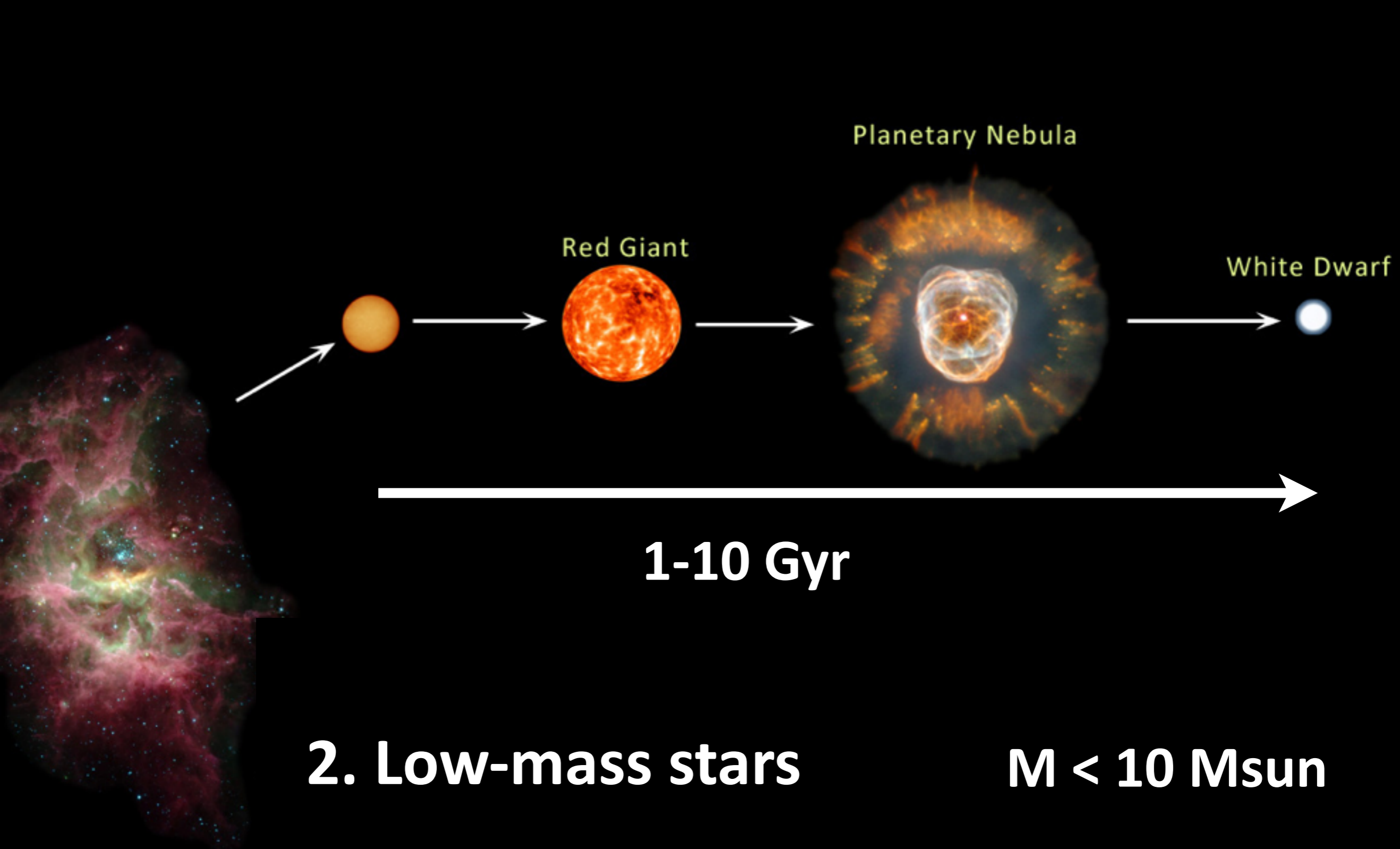
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Electrons do not become degenerate



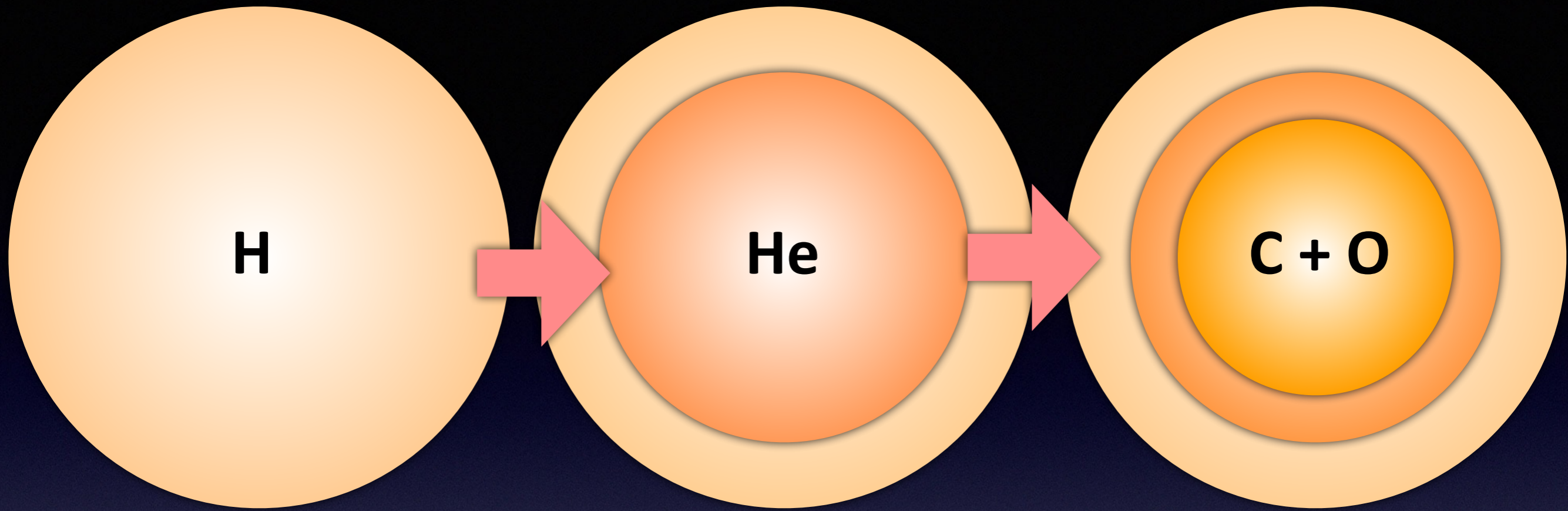
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2. Low-mass stars

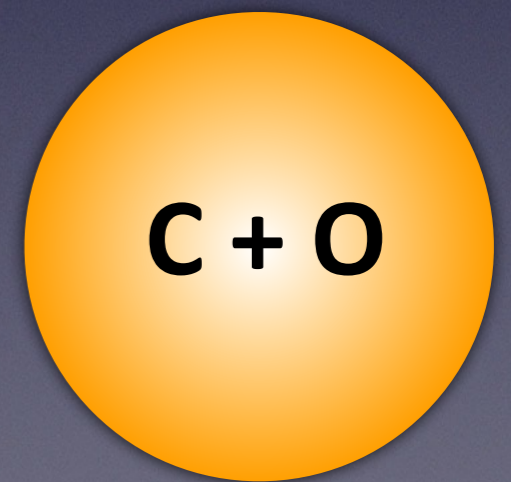
$M < 10 M_{\text{sun}}$

Stellar Cloud
with
Protostars



Stars can be supported by
electron degeneracy pressure

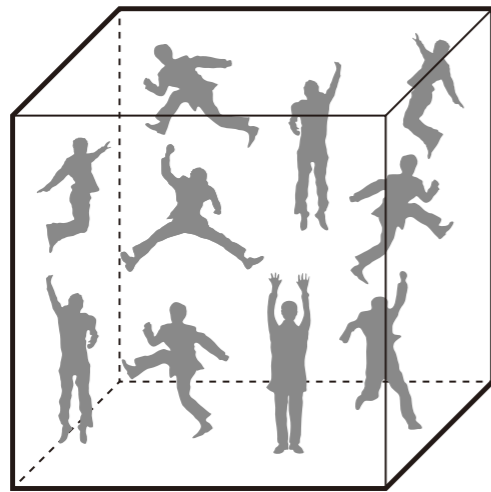
White dwarf



White dwarf: supported degeneracy pressure

普通の気体の圧力

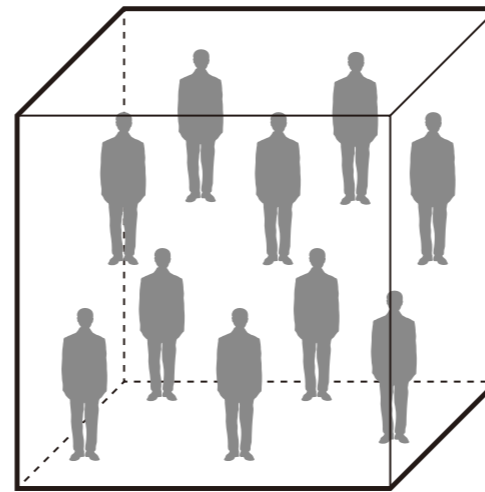
Ideal gas



温度を下げる



T decreases



圧力が下がる

縮退圧

Degeneracy pressure



温度がゼロでも圧力が生まれる

**P is non-zero
even at T=0**

星が「死ぬ」とはどういうことか
(ベレ出版)

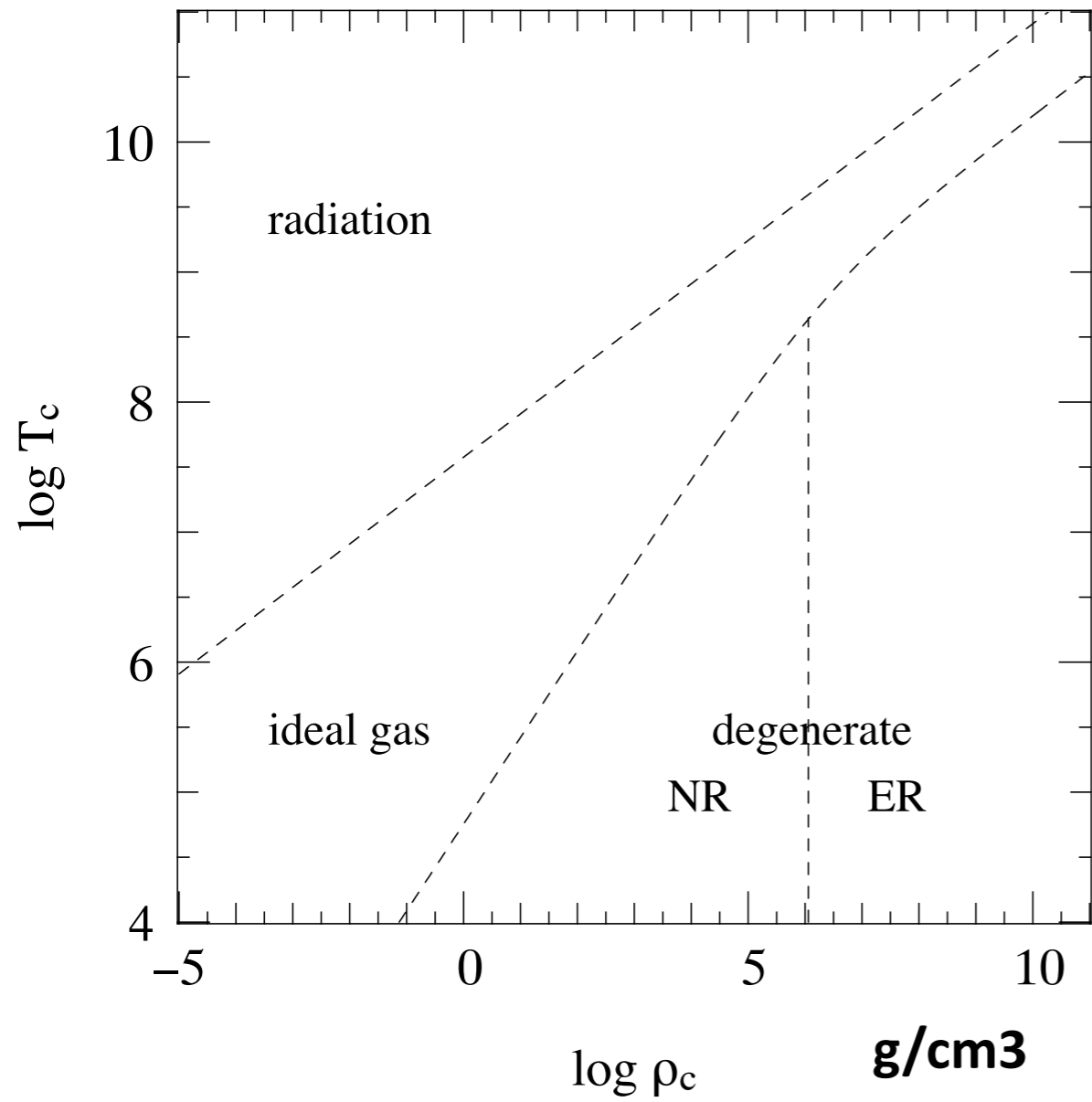
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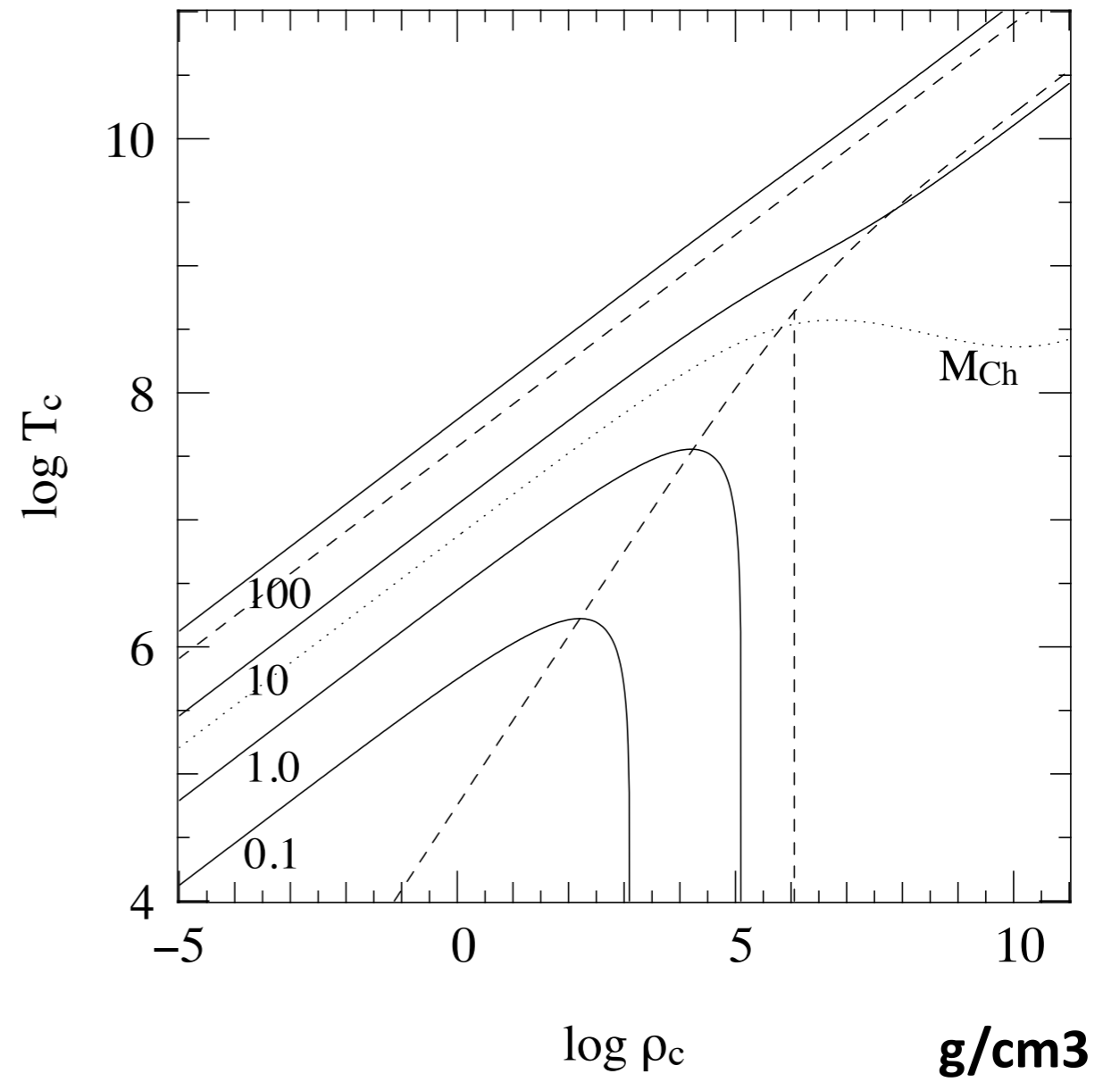
5.1 Equation of state

5.2 Evolutionary track

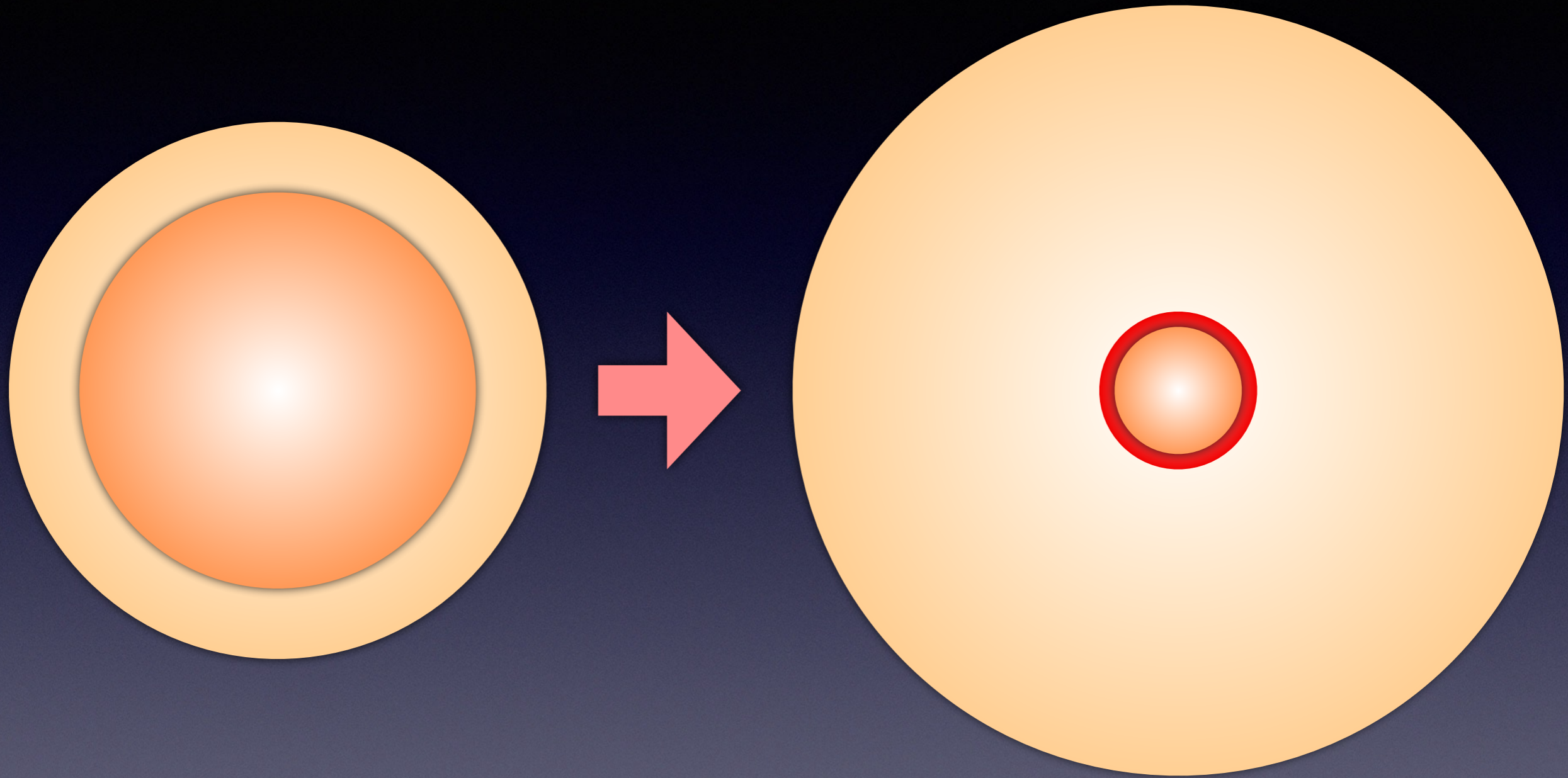
EOS



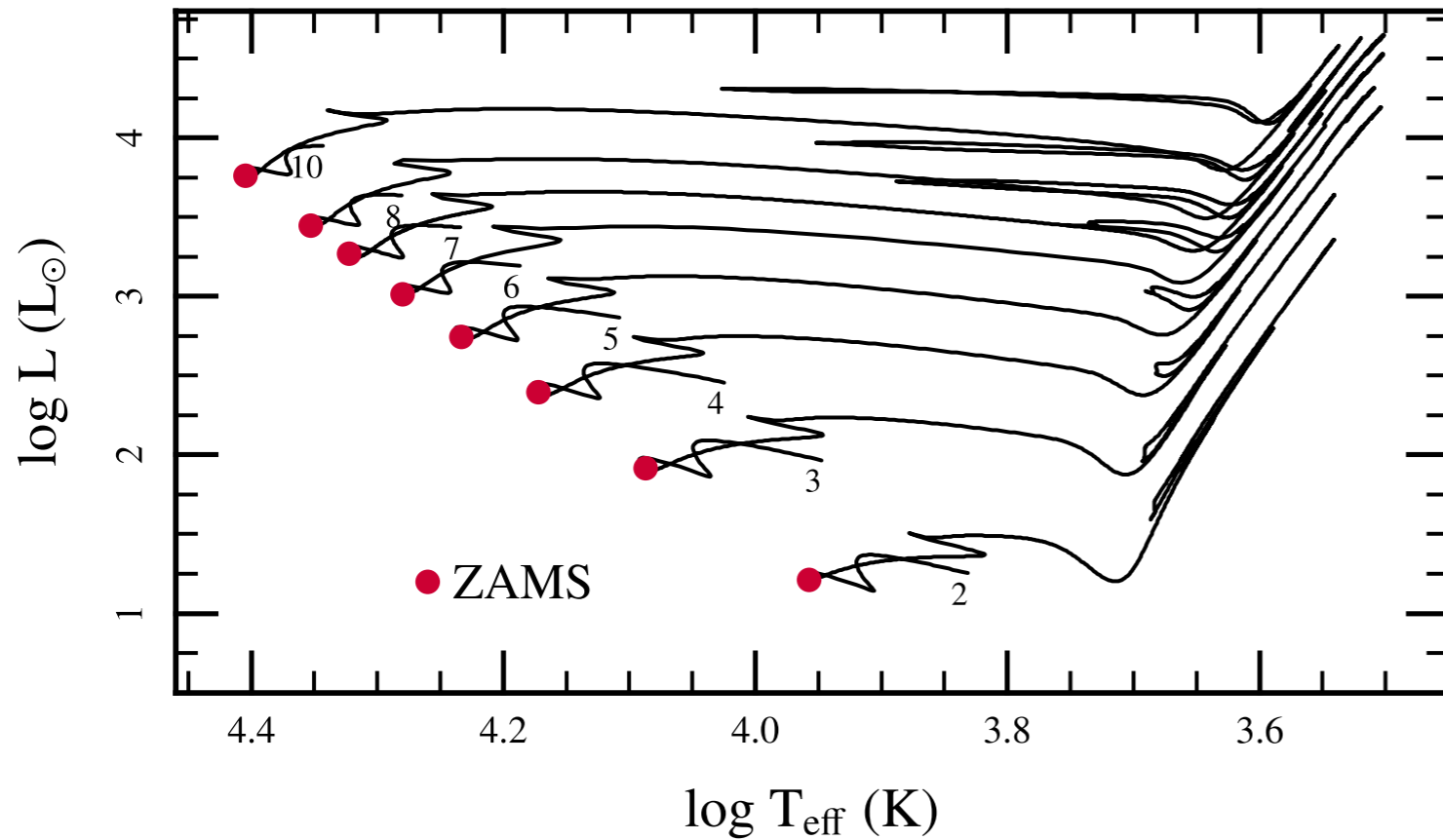
Evolution of T_c and ρ_c



**Contraction of the core
= Expansion of the envelope**

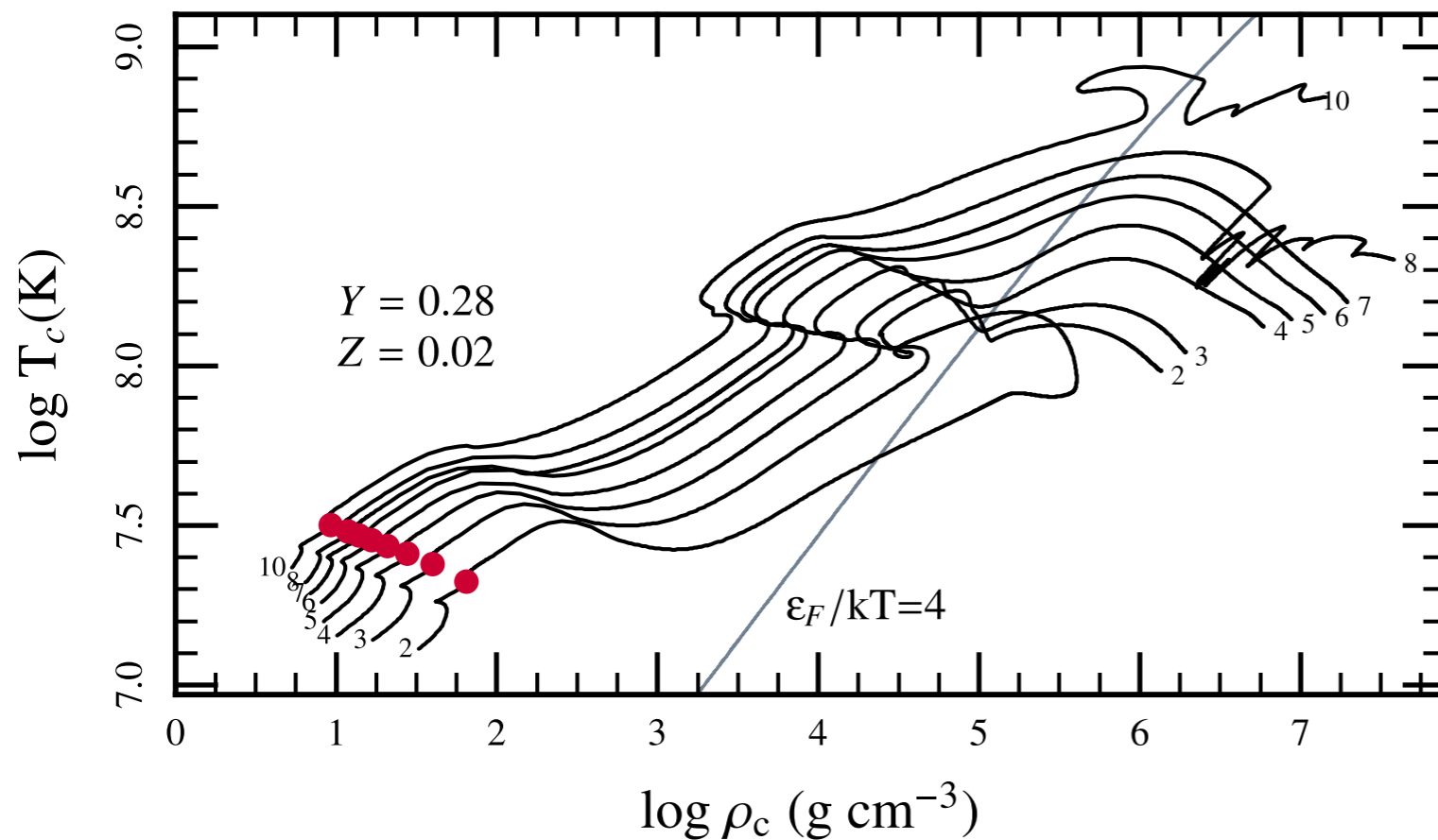


**Shell burning => energy generation
(more than required to support the envelope)**

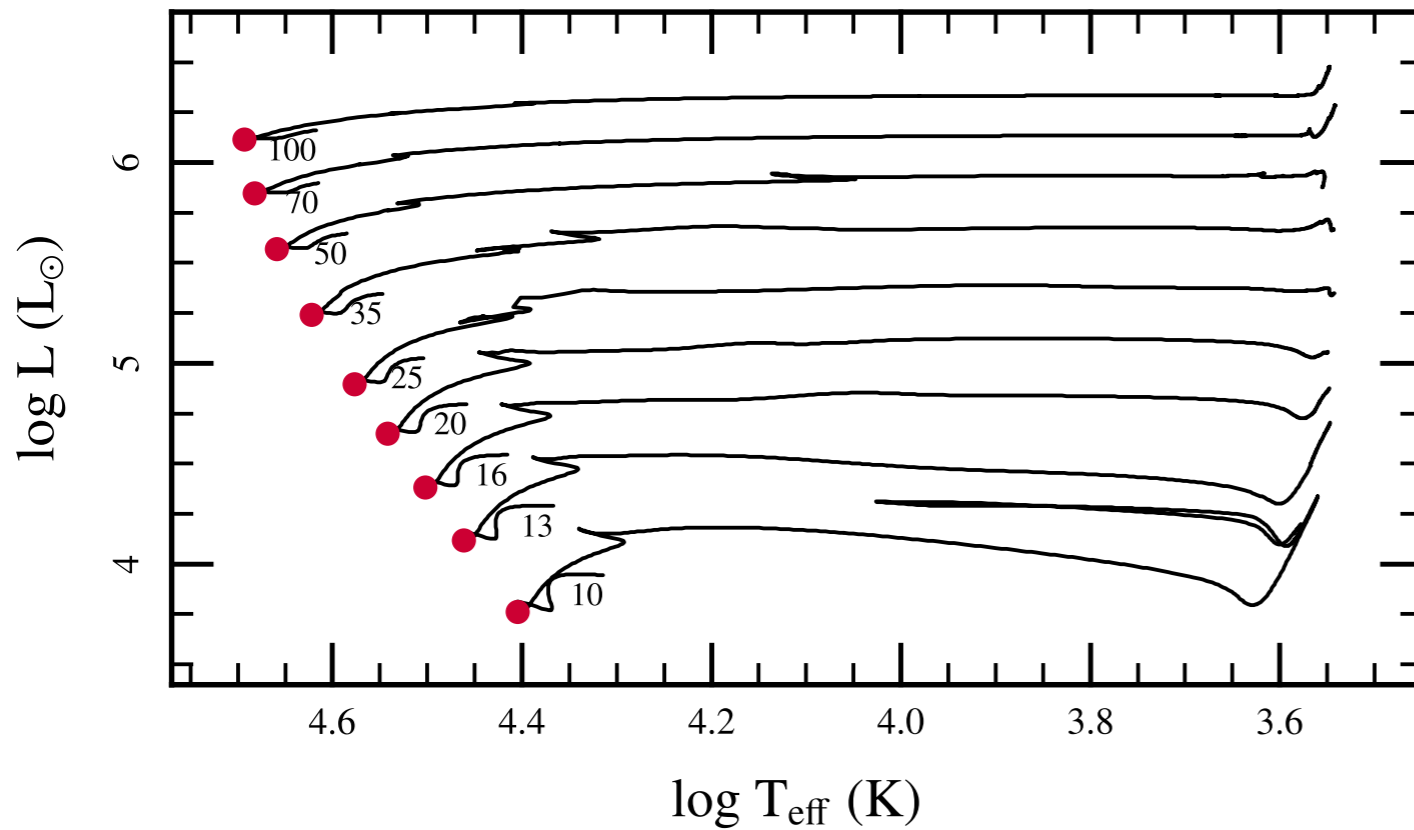


Low/intermediate
mass stars

Core contraction
=> Expansion of the envelope
=> Red giant

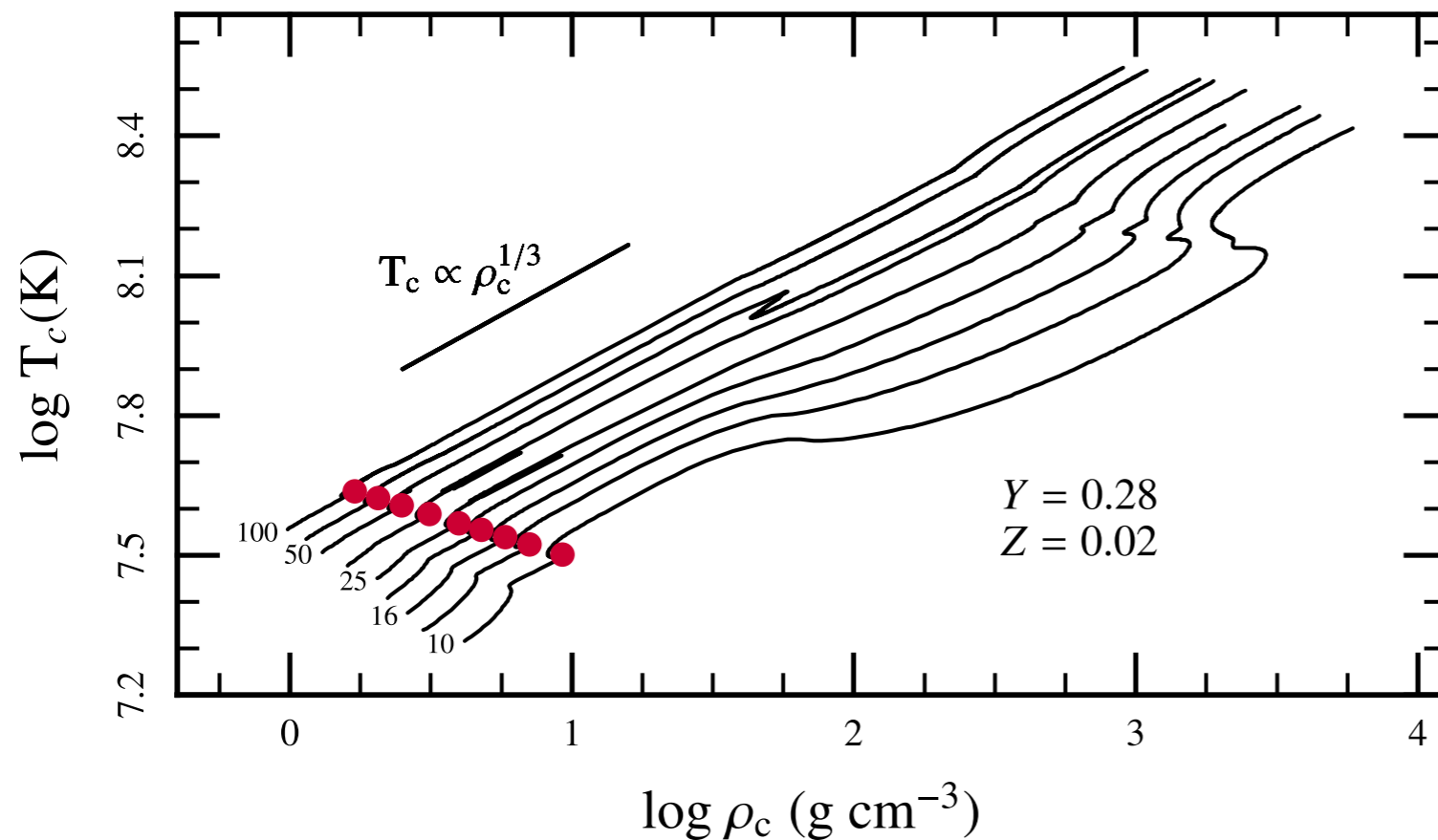


Paxton et al. 2011

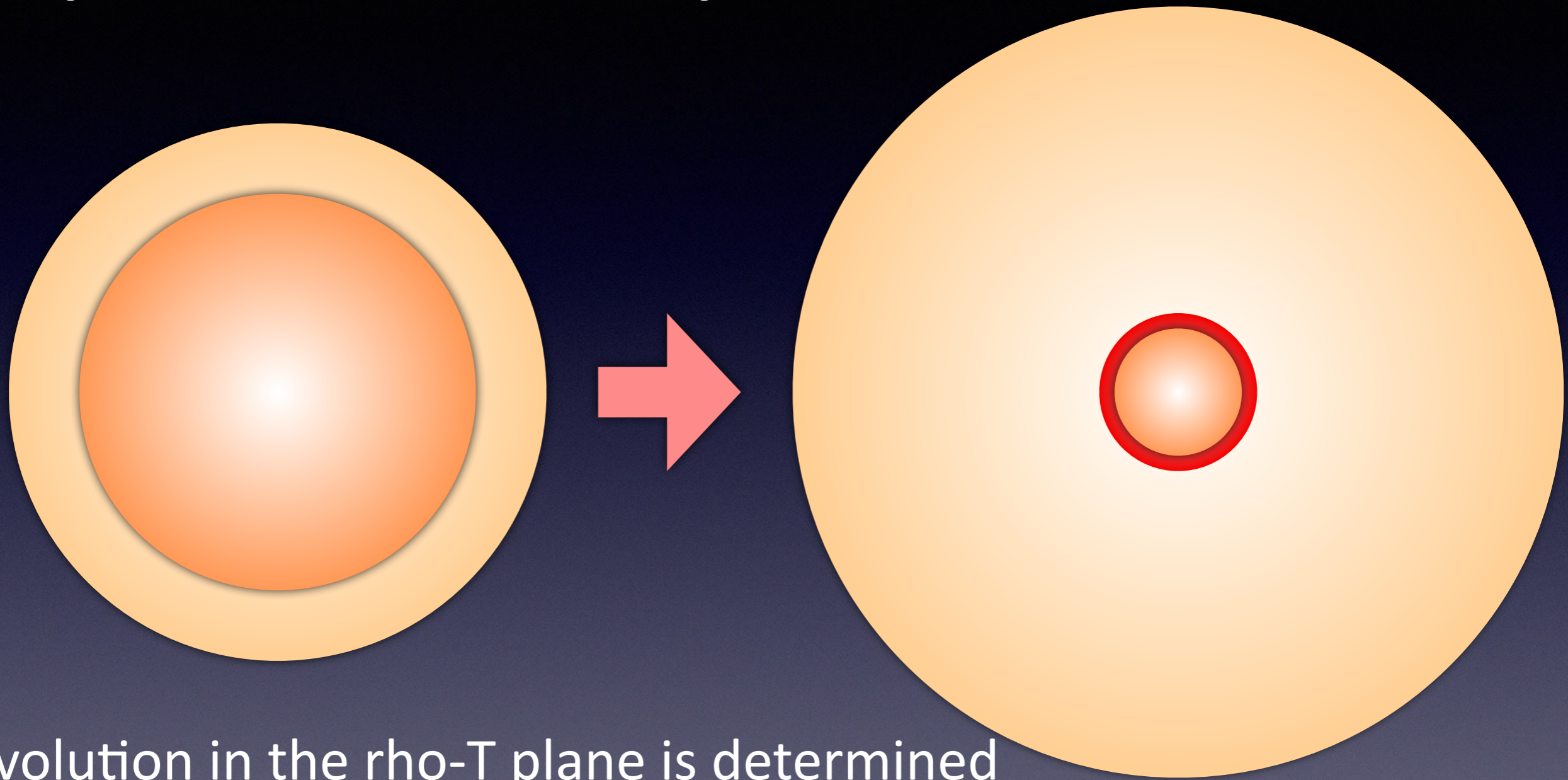


**Massive stars
(until He-burning)**

**Core contraction
=> Expansion of the envelope
=> Red super giant**



**Contraction of the core
= Expansion of the envelope**



Evolution in the ρ - T plane is determined
by the properties of the core

$$T \sim M^{2/3} \rho^{1/3}$$

M decreases \Rightarrow Lower part of the ρ - T plane

Summary: stellar evolution (II)

- **Properties of gas (microscopic)**
==> **properties of stars (macroscopic)**
- **Equation of states**
 - Ideal gas $P \sim \rho T$
 - Degeneracy pressure $P \sim \rho^{5/3}$ (non-rel), $P \sim \rho^{4/3}$ (rel)
 - Radiation pressure $P \sim T^4$
=> Important in different areas in the rho-T diagram
- **Stellar evolution**
 - Stars stop contraction when supported by degeneracy pressure
=> No temperature rise => End of nuclear burning
 - The core of low mass stars become generate

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Thermodynamics

Electromagnetism

**Classical
mechanics**

**Statistical
mechanics**

Astrophysics

Hydrodynamics

**Quantum
mechanics**

Relativity

Nuclear physics